

# Lattice dynamics calculation of infrared active modes of cuprate superconductors

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## Abstract

We have calculated the highest-energy infrared active  $E_u$  mode for three cuprate compounds with and without apical ions, in order to investigate the experimental energy-difference between T- and T'-structures. The calculated energies show the similar Cu-O bond length dependence to the experimental results. The calculated spin densities of the T-structure have more electrons in the  $d_{x^2-y^2}$  orbital than that of the T'-structure. This means that the  $\text{CuO}_2$  plane in the T-structure is compressed, in comparison with the T'-structure even with the same Cu-O bond length. This compression increases the energy of the  $E_u$  mode in the T-structure. This is the clear evidence that the block layer is important for the electric state on the  $\text{CuO}_2$  plane.

*Key words:* *ab-initio* calculation, phonon, cuprate, apical oxygen

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Recently we have reported that the highest-energy infrared active  $E_u$  mode has larger energy by  $45\text{cm}^{-1}$  for the T-structure cuprates than that for the T'-structure ones even with the same Cu-O bond length[1]. This mode is the stretching vibration of the Cu-O bond along the  $\text{CuO}_2$  plane. This energy difference suggests that the electric state in the  $\text{CuO}_2$  plane is different between them, since this mode has the same atomic displacement for both structures. To investigate a relationship between this energy difference and the electric state, we performed first-principles calculations of lattice vibrations at  $q=0$  for three compounds, i.e.  $\text{La}_2\text{CuO}_4$  with T-structure (abbreviated by T-LCO),  $\text{Sr}_2\text{CuO}_2\text{Cl}_2$  with T-structure (T-SCOC), and  $\text{La}_2\text{CuO}_4$  with hypothetical T'-structure (T'-LCO).

The present results were obtained by the ABINIT code [2], which is based on *ab-initio* pseudopotentials and a plane-wave basis set in the framework of the density-functional formalism. All calculations were

performed with the local spin density approximation (LSDA) parameterized by Perdew and Wang [3]. The space group Bmab was used for all calculated compounds to produce an antiferromagnetic order in the  $\text{CuO}_2$  plane. The phonon energy was calculated by the density functional perturbation theory [4]. At the first step, the optimized structures were calculated in the space group Bmab and then we proceeded phonon calculations using these structures.

The optimized lattice structures of T-SCOC and T'-LCO are consistent with the symmetries of ideal T- and T'- structure even if the symmetry of Bmab was assumed in the calculations. The calculated structures show good agreement with the experimental results for T-LCO and T-SCOC, and the difference in the lattice constants and atomic positions between the calculated and experimental results is less than 3%. The calculated energies of the  $E_u$  mode are shown in Fig. 1, where the reported experimental results are also plotted. In the figure, we draw four lines with the same slope of  $1.78 \times 10^3 \text{cm}^{-1}/\text{\AA}$ . The calculated results is plotted by dotted lines and the experimental ones solid lines for

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both T- and T'-structures. All data are on the corresponding lines. The same energy difference of  $45\text{cm}^{-1}$  between T-structure and T'-structure are found for both calculated and experimental results. We note the absolute energy difference of  $30\text{cm}^{-1}$  between the calculations and the experiments is caused by the energy determination accuracy in the calculation. This accuracy is the same for the T- and T'- structures. Thus, this result shows the calculation can reproduce correctly the experimental Cu-O bond dependence.

In order to discuss the origin of the energy difference, we have also calculated spin densities of T-LCO and T'-LCO and the results are shown in Fig. 2. The spin density corresponds to the density of the hole wavefunction, since only one electron plays a dominant role for the  $\text{Cu}^{2+}$  case. As clearly seen, the hole wavefunction in T-LCO includes small amount of  $d_{3z^2-r^2}$  orbital, while that in T'-LCO is almost  $d_{x^2-y^2}$  orbital. This means that a small amount of electronic charge is transferred from  $d_{3z^2-r^2}$  to  $d_{x^2-y^2}$  orbitals due to the existence of the apical ions in the T-structure. This electronic charge transfer increases the Cu-O bond length in the  $\text{CuO}_2$  plane in terms of Jahn-Teller distortion. However, the Cu-O bond length can not be freely relaxed, since the length is determined only by optimization of energy against the size of the block layer. In fact, the Cu-O bond length in the T-LCO is shorter than that in the T'-LCO. These facts indicate that the  $\text{CuO}_2$  plane in the T-structure is compressed in comparison with that in the T'-structure even with the same Cu-O bond length. This compression increases the  $E_u$  mode energy in the T-structure. The present results clearly show the importance of the block layers on the electric state at the  $\text{CuO}_2$  plane through their size and charge distribution.

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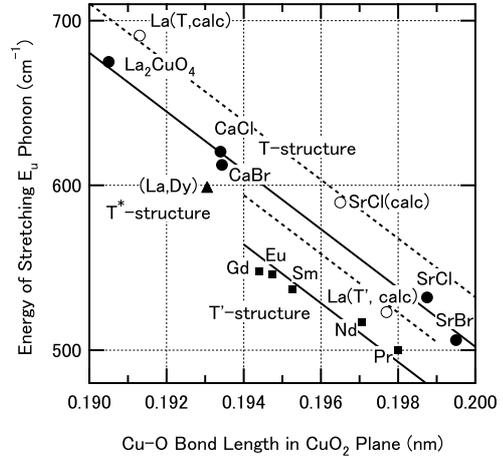


Fig. 1. Bond length dependence of the energy of the stretching Cu-O vibration along the  $\text{CuO}_2$  plane. The closed circle, triangle, and square symbols are experimental data for T-structure, T\*-structure, and T'-structure, respectively, taken from Refs. [1], [5], and [6]. The open circle symbols are calculated results. For  $\text{R}_2\text{CuO}_4$  compounds, only rare earth ion R is presented, while for  $\text{R}_2\text{CuO}_2\text{X}_2$  compounds they are abbreviated by RX.

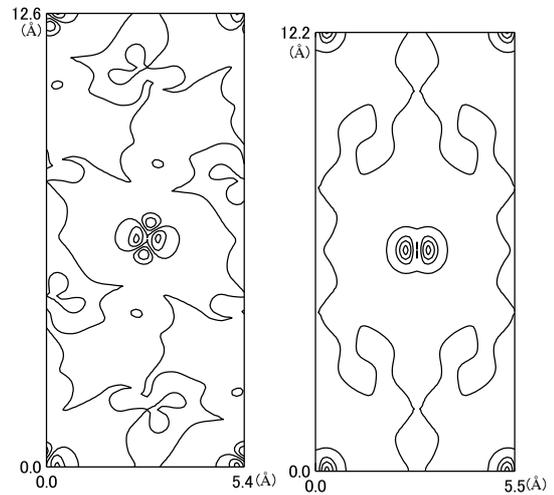


Fig. 2. The spin densities of T-LCO (left) and T'-LCO (right) on ac-plane. The Cu ions locate on center and corners. The contours are drawn by the interval of  $0.01 \mu_B/\text{Bohr}^3$ .