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Title	Comparison of diesel spray with small injection amount between single-hole and multi-hole injectors: Results under same rail pressure and similar injection rate
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Relation	

1 Comparison of Diesel Spray with Small Injection Amount between Single-hole and
2 Multi-hole Injectors: Results under Same Rail Pressure and Similar Injection Rate

3

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8

9 **Abstract**

10 A comparison of diesel spray for injectors with single-hole (SH) and multi-hole (MH)
11 nozzles has been conducted under same rail pressure and similar injection rate (30
12 MPa for SH and 100 MPa for MH) conditions. The result showed that the spray of SH
13 injector has a longer penetration under same rail pressure condition caused by the
14 faster build-up process of sac pressure. The spray of MH injector has a larger spray
15 angle resulted from the complicated nozzle flow. These further affect the
16 evaporation rate and mixture formation process. Regarding the same rail pressure
17 condition, the spray of SH injector shows a fast evaporation rate, as well as the MH
18 injector, although the spray angle of SH injector is quite small. For the entire mixture
19 formation process, more spray vapor of SH is distributed in the thin area. For similar

20 injection rate condition, the effect of different spray tip penetration can be
21 eliminated while the advantage of the large spray angle of MH injector becomes
22 apparent. The evaporation rate and mixture formation process of the SH injector are
23 much worse than those of the MH injector. The complex nozzle internal flow of MH
24 injector is responsible.

25 Keywords: Diesel; Spray; Single-hole; Multi-hole; Evaporating

26

27 **1. Introduction**

28 The spray behavior and mixture formation process in the engine cylinder play a
29 decisive role in diesel engines. Since emission formation and engine performance are
30 mainly controlled and determined by mixture status. Various research activities have
31 been carried out on diesel spray for the common-rail injectors.

32 There are many visualization methods can be used to obtain the spray behavior. The
33 most general method is to fix the injectors into a vessel (or constant volume
34 chamber). The fuel is injected into the vessel which with the pre-defined ambient
35 pressure and temperature. A single-hole (SH) injector has been widely used for
36 experimental research, since it has a better optical observation and comprehensive
37 study. In additional, the independent effects of the individual parameters are much
38 easier to be clarified. Since the spray plume of SH injectors does not have the issues

39 of optical path blocking and adjacent plume interference.

40 However, in a real engine, the injectors widely used are MH ones. Therefore, it is
41 necessary to make sense of the difference of sprays between SH and MH types.

42 Different nozzle flow characteristics inside sac are one of the crucial reasons lead to
43 the spray behavior significantly different, especially when the needle lift is very low.

44 The holes of SH injectors are located at the end of nozzle. Nevertheless, the holes of
45 MH injectors are located at the side of the sac. The studies have shown that, nozzle
46 flow state is directly linked with the location of the holes relative to the sac. ^{(1),(2)}
47 besides, nozzle flow can be altered by needle lift dramatically.⁽³⁾⁻⁽⁷⁾ The flow
48 streamline inside nozzle is determined by needle lift. Initially, a low needle lift usually
49 guides the flow into the sac directly. Then, fuel flows into the hole inlet from sac.

50 Compared with SH injectors, a higher radial direction velocity can be created by the
51 vortex formed inside the holes of MH injectors. As a result, MH injector has a larger
52 spray angle caused by higher radial velocity.

53 The comparison between SH and MH injectors has been conducted by various
54 studies under quasi-steady state conditions;⁽⁸⁾⁻⁽⁹⁾ few studies concentrate on the
55 spray with transient variation, such as low needle lift and small injection mount cases.

56 It is also very important to investigate the spray behavior under quite small injection
57 amount, since small injection amount represent the sprays of pilot injected fuel of a

58 real engine. Because of the greatly influences of low needle lift on the upstream flow
59 state of holes, it is meaningful to conduct a comparison of mixture formation process
60 between SH and MH injectors. Prior to the small injection amount, a comparison had
61 been conducted for the quasi-steady spray (large injection amount) and has been
62 published in SAE World Congress 2019.⁽¹⁰⁾

63 The pressure-drop between the sac volume and the ambient gas actually controlled
64 by the exit velocity. The pressure build-up process of sac volume for SH and MH
65 injectors would be different under same rail pressure condition. That is caused by the
66 different flow rates and areas of SH and MH injectors. Therefore, in addition to the
67 contents mentioned above, the injection pressure of the SH injector was adjusted
68 accordingly to match the injection rate of both injectors equal. The influence of the
69 difference of the sac pressure can then be negligible between two injectors. The
70 mixture formation process was analyzed again under such condition, as well as the
71 nozzle internal flow and near-field spray simulation. Then, another comparison of
72 spray behavior of both injectors under different injection control parameters can be
73 conducted. This can further provide an insight into priority of the controlling
74 parameters when conducting experiments with an SH injector as the substitute of a
75 MH injector.

76 **2. Investigation Method**

77 2.1 LAS Principle and experimental setup

78 The different attenuation between visible (Vis) and ultraviolet (UV) light is the basic
79 principle of the Laser Absorption and Scattering (LAS) technic. Therefore, we can
80 obtain the concentration of vapor and liquid phases by comparing the attenuation of
81 Vis and UV lights. The UV light intensity can be attenuated by both the vapor and
82 liquid phases. The attenuation of liquid phase is caused by droplet scattering and
83 absorption. The attenuation of vapor phase is caused by vapor absorption. While, the
84 attenuation of Vis light is only caused by the droplet (liquid phase) scattering. This
85 phenomenon could be expressed by the Eqs. (1) and (2), respectively:

$$86 \quad \log (I_0/I_t)_{\lambda_A} = \log (I_0/I_t)_{L_{sca}} + \log (I_0/I_t)_{L_{abs}} + \log (I_0/I_t)_{V_{abs}} \quad (1)$$

$$87 \quad \log (I_0/I_t)_{\lambda_T} = \log (I_0/I_t)_{L_{sca}} \quad (2)$$

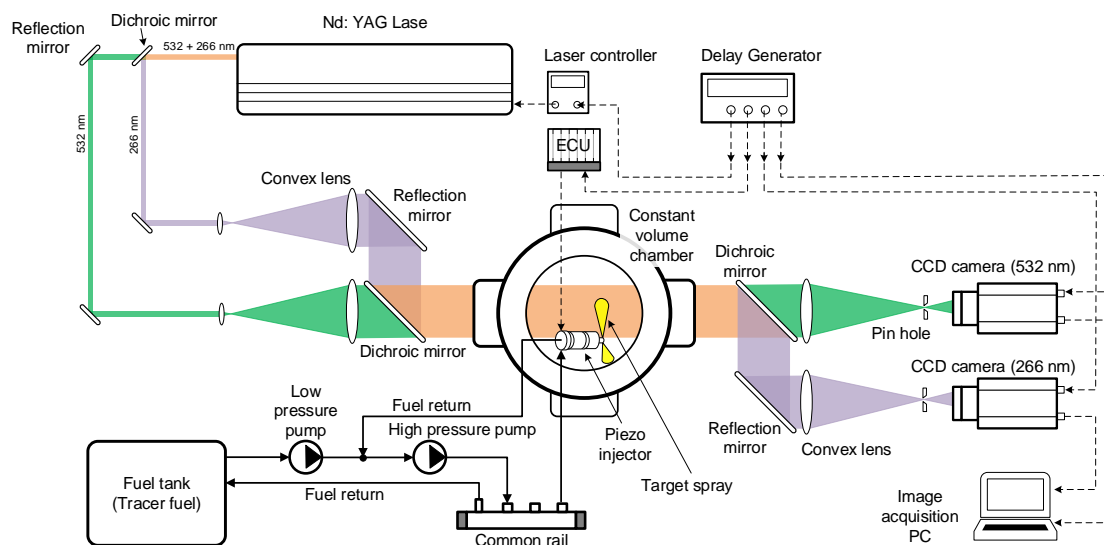
88 where $\log (I_0/I_t)_{\lambda_A}$ and $\log (I_0/I_t)_{\lambda_T}$ are the total optical thickness of UV and
89 visible lights, which represent the attenuation of each light intensity. $\log (I_0/I_t)_{L_{sca}}$,
90 $\log (I_0/I_t)_{L_{abs}}$ and $\log (I_0/I_t)_{V_{abs}}$ represent the attenuation caused by the droplet
91 scattering, droplet absorption and vapor absorption. Since $\log (I_0/I_t)_{L_{abs}}$ can be
92 ignored in Eq. (1). Therefore, vapor absorbance can be calculated by Eq. (3):

$$93 \quad \log (I_0/I_t)_{V_{abs}} = \log (I_0/I_t)_{\lambda_A} - \log (I_0/I_t)_{\lambda_T} \quad (3)$$

94 The experimental setup schematic is showed in Figure 1. Two Charge Coupled Device
95 (CCD) cameras and a pulsed ND-YAG laser are used for the optical system. The

96 wavelength of 266 nm and 532 nm are used for UV and Vis, respectively. Firstly, The
 97 UV and Vis lights are expanded to the size similar with the optical window (quartz) of
 98 the chamber. Then, merged lights pass through the spray inside the chamber.
 99 Subsequently, the lights, which have been attenuated by the spray, are separated
 100 again by a light splitter and captured by CCD cameras. The mass distributions and
 101 equivalence ratios of vapor and liquid phases can be analyzed base on vapor and
 102 liquid absorbance by employing Bouguer-Lambert-Beer's law⁽¹¹⁾. More details of LAS
 103 technic can be found in previous literatures. (12)–(14)

104



105

106

Figure 1 Schematic of experimental setup

107 A blended fuel (tracer fuel) of α -methyl-naphthalene (2.5%) and n-tridecane (97.5%)
 108 is used in the experiment. The physical properties of tracer fuel are listed in Table 1.
 109 The tracer fuels selection and its requirements for LAS technic can be found in

110 previous literature⁽¹²⁾.

111 Table 1 Properties of the test fuel

Items	Blended fuel α -MN (2.5%), n-tridecane (97.5%)
Density [kg/m ³]	767
Boiling point [K]	509
Kinematic viscosity [mm ² /s]	2.48

112

113 For one injection event, with the aim of reducing the noises during the image

114 processing, an interval of 0.5 sec were set between images of background and spray.

115 The injection interval and the imaging timings were controlled by a delay generator.

116 The imaging moments were determined by this interval during one injection event.

117 Table 2 list the specification of the injectors adopted in this work. The nozzles of two

118 injectors have identical geometry, except that the umbrella angle (included angle) for

119 the MH injector is 155 degrees. In order to obtain the sprays that the spray axis

120 parallel to the imaging plane, the chamber cover was carefully designed for MH

121 injector (Figure 2). The MH injector is tilted 45° and arranged eccentrically on the top

122 of the cover. The target spray (parallel to imaging plane) has an angle of 17.2° with

123 horizontal plane. Unfortunately, as the observation issues for MH injector mentioned

124 previously, the area within 9mm of the hole exit is invisible.

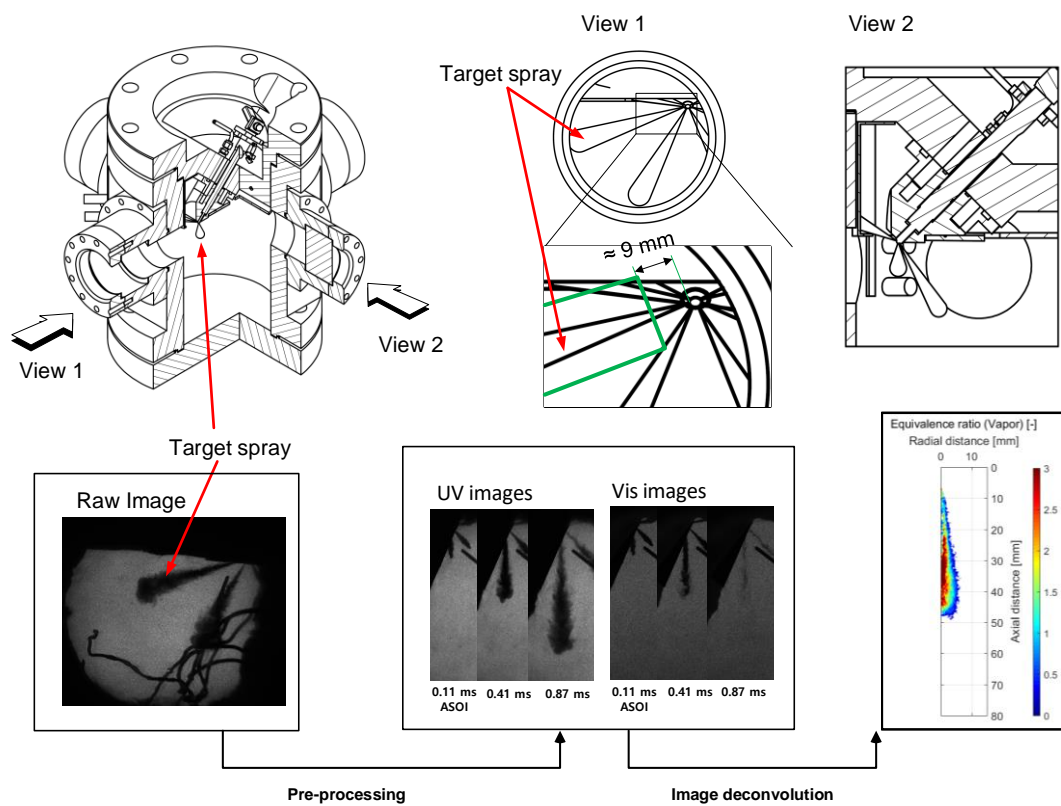
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126

Table 2 The injectors specification

Items	SH	MH
Type of injector [-]	Piezo-type	
holes Number [-]	1	7
Hole diameter at exit [mm]	0.123	
Hole length [mm]	0.8	
K-factor [-]	2.7	
Umbrella angle [deg.]	-	155

127



128

129 Figure 2 The multi-hole injector arrangement for axisymmetric spray, and the

130 sequence for image-processing

131 Table 3 summarized the experimental conditions. For better understanding, the

132 injection amounts have been normalized to the mass injected per hole throughout

133 this paper. A typical condition in-cylinder with a high temperature and low density

134 was selected for the ambient condition at the end of compression stroke. The aim of
 135 selecting this condition is to simulate the vicinity injection condition at the pilot
 136 timing. For the same rail pressure condition, the rail pressure and injection amount
 137 were 100 MPa and 0.5 mg/hole, respectively. For similar injection rate condition, the
 138 rail pressure of the SH injector was adjusted to 30 MPa to achieve a similar injection
 139 rate as the MH injector.

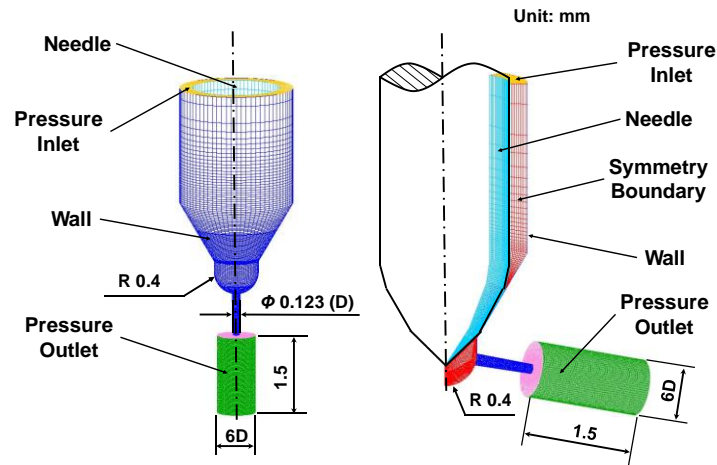
140 Table 3 Experimental conditions

Items	SH	MH
Ambient pressure [MPa]	2.0	
Ambient density [kg/m ³]	8.4	
Ambient temperature [K]	800	
Same rail pressure		
Injection amount [mg/hole]	0.5	
Rail pressure [MPa]	100	
Similar injection rate		
Injection amount [mg/hole]	0.53	0.59
Rail pressure [MPa]	30	100

141 **2.2 Numerical setup of CFD simulation**

142 In the simulation section, two simplified nozzles which have same nozzle tip
 143 geometries with the experiment section were employed for analyzing the flow state
 144 inside the holes of nozzle and near-field behavior. As shown in Figure 3, the entire
 145 nozzle tip is modeled for the SH injector, while one-seventh (one hole) of the nozzle
 146 tip is selected for MH injector. In addition, a cylindrical cavity with a length of 1.5 mm
 147 and a radius of 3 times the hole diameter is set at each hole exit to maintain a stable

148 ambient pressure.



149

150

Figure 3 Nozzle structure, meshes and boundary conditions

151

Commercial software AVL Fire (Ver. 2014) was employed for this numerical

152

calculation. The fluids property, boundary conditions and models are summarized in

153

Table 4. The ambient condition and injection pressure of simulation are same with

154

the experiment for similar injection rate. The four-equation model $k-\zeta-f$ of RANS

155

method and multi-fluid model are selected as the turbulence and multiphase flow

156

model, respectively. The Linear Cavitation model based on Rayleigh equation⁽¹⁵⁾ is

157

adopted for depicting the cavitating flow, and its Mass Exchange is described below:

158

$$\Gamma_v = \rho_l N 4\pi R^2 \dot{R} = -\Gamma_l \quad (4)$$

159

where N represent bubble number density, R represent bubble radius, v is vapor

160

phase (diesel vapor) and l is liquid phase (diesel).

161

Table 4 Fluids property, conditions and models in simulation

Items	SH	MH
Commercial software	AVL Fire (Ver. 2014)	

Diesel	Density (kg/m ³)	830	
	Viscosity (N·s/m ²)	0.00214	
Vapor	Density (kg/m ³)	7	
	Viscosity (N·s/m ²)	10 ⁻⁵	
Air	Density (kg/m ³)	17.4	
	Viscosity (N·s/m ²)	1.8×10 ⁻⁵	
	Inlet Pressure (MPa)	30	100
	Outlet Pressure (MPa)	0.75	
	Temperature (K)	300	
	Turbulence Model	k- ζ -f	
Cavitation Model	Linear Cavitation Model	-	
	Cavitation Bubble Density	1.0×10 ¹²	
	Saturated Vapor Pressure (Pa)	892	
	Needle-holder gap (μ m)	2	
	Cell size around the hole (μ m)	2.7	2.6

162

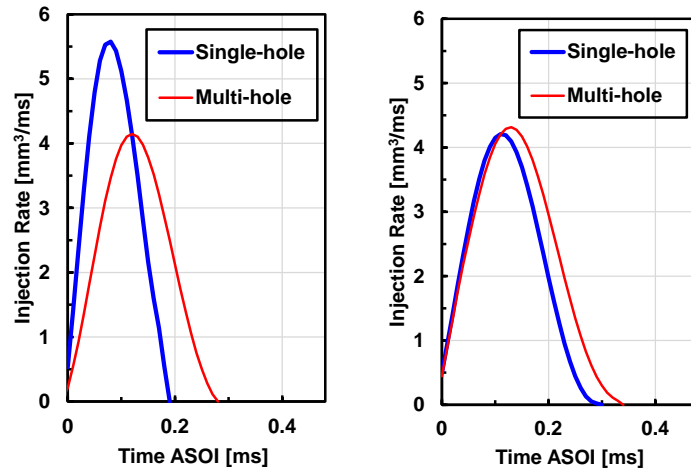
163 3. Results and discussions

164 3.1 Evaporating spray characteristics

165 For better understand the experimental content of this paper, the authors would like
166 to show the injection rate of SH and MH injectors under both same rail pressure and
167 similar injection rate conditions (Figure 4) firstly. The injection rate profiles were
168 measured by ONO SOKKI FJ7000 Injection Measuring System which is based on
169 Zeuch's method.^{(16),(17)(17)}

170 As shown in Figure 4(a), The injection rate curve of SH injector increased much faster
171 than that of MH injector during the rising period. This implies that the SH injector has
172 a larger exit velocity, which makes the spray parameters of injectors greatly different.

173 In order to eliminate the impact of the exit velocity on spray characteristics, authors
 174 achieved a similar exit velocity magnitude of the SH and MH injectors by adjusting
 175 the rail pressure, and got the injection rate profiles as shown in Figure 4(b). The rail
 176 pressure of SH injector is 30 MPa, and that of MH injector is 100 MPa.



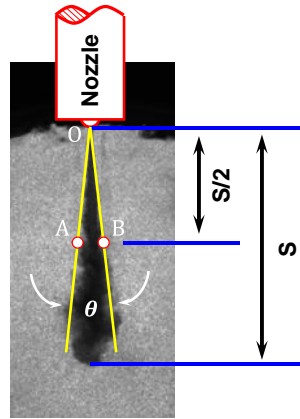
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178 (a) Same rail pressure of 100MPa (b) Similar injection rate

179

Figure 4 Injection rate.

180 Before the discussion of spray characteristics, the authors first focus on two
 181 definitions of spray parameters, which are very important and fundamental
 182 parameters that directly represent spray diffusion and fuel-air mixing processes
 183 (Figure 5). Spray tip penetration S is defined as the length from nozzle tip to spray tip.
 184 The angle $\angle AOB$ names spray angle is defined as the angle between the nozzle tip
 185 and the spray boundary at the half S .



186

187

Figure 5 Spray tip penetration and spray angle definitions.

188

Figure 6 shows the spray tip penetration of the SH and MH injectors under both

189

same rail pressure and similar injection rate conditions. Due to the smaller total exit

190

cross-sectional area (one-seventh of the MH injector), the sac pressure of SH injector

191

increases significantly faster, which leads to a larger velocity at the hole exit of SH

192

injector. This is why the SH injector has a larger spray tip penetration, which would

193

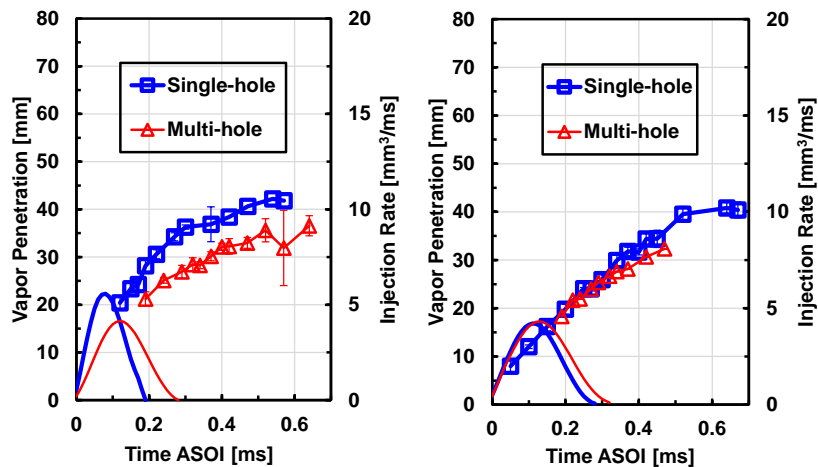
lead to more air entrainment. As for the similar injection rate condition, the spray tip

194

penetrations for SH and MH injectors show a great coordination before the end of

195

injection caused by the similar injection rate and exit velocity.

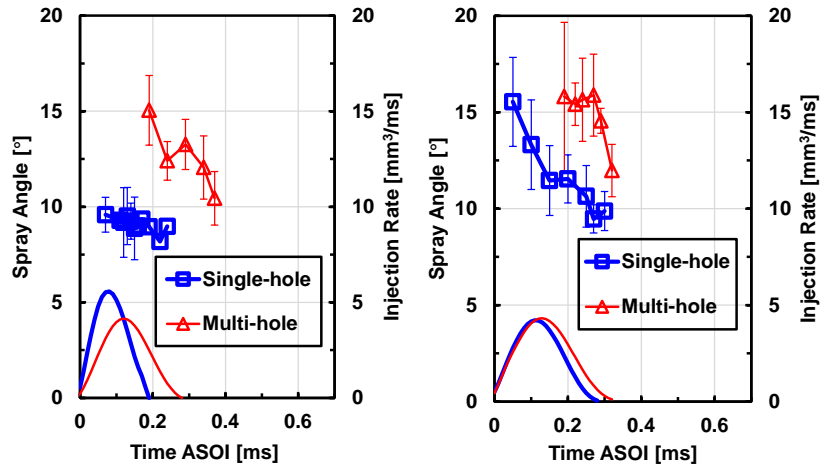


196

197 (a) Same rail pressure of 100MPa (b) Similar injection rate

198 Figure 6 Spray tip penetration (vapor) under same rail pressure of 100 MPa and
199 Similar injection rate.

200 For a certain diesel injector, as we all know, spray angle and tip penetration mainly
201 determined by the rail pressure and ambient density. Generally, the faster the spray
202 tip penetration increases, the smaller the spray angle is under the constant ambient
203 condition. While for diverse types of injectors, the situation will be quite different
204 since difference existing in various parameters, such as hole geometry, hole location,
205 sac volume, and needle tip geometry. In the comparison of SH and MH, both the hole
206 location and the total sectional area of holes were taken into consideration.
207 Obviously, as shown in Figure 7(a), the spray of SH injector has a much smaller spray
208 angle. Of course, the faster hole exit and spray tip velocities made a lot of
209 contributions on it. However, if we shift our focus to the similar injection rate
210 condition, we can find a similar scene in Figure 7(b). The spray angles of the SH and
211 the MH injectors still maintains a large gap. As described above, SH and MH injectors
212 have similar injection rate, exit velocity and spray tip penetration. That means hole
213 location has a greater impact on spray angle than spray tip penetration (exit velocity).
214 Therefore, nozzle internal flow plays a significant role on spray angle and will be
215 further discussed in simulation section.



(a) Same rail pressure of 100MPa (b) Similar injection rate

Figure 7 Spray angle.

216

217

218

219 It is well known that equivalence ratio, as a crucial factor of combustion process, is

220 an extremely important indicator of engine performance and exhaust emission. With

221 the rise of new combustion modes such as HCCI and PCCI, the requirements for the

222 equivalence ratio of mixture formation and combustion process are becoming higher

223 and higher. Both excessively rich and lean mixtures would be likely to cause

224 undesired situations during engine operation. However, the difference between the

225 equivalence ratio of SH and MH injector is not clear at present. It is not appropriate

226 to apply the experimental results of the SH injector to the real engine. Therefore, the

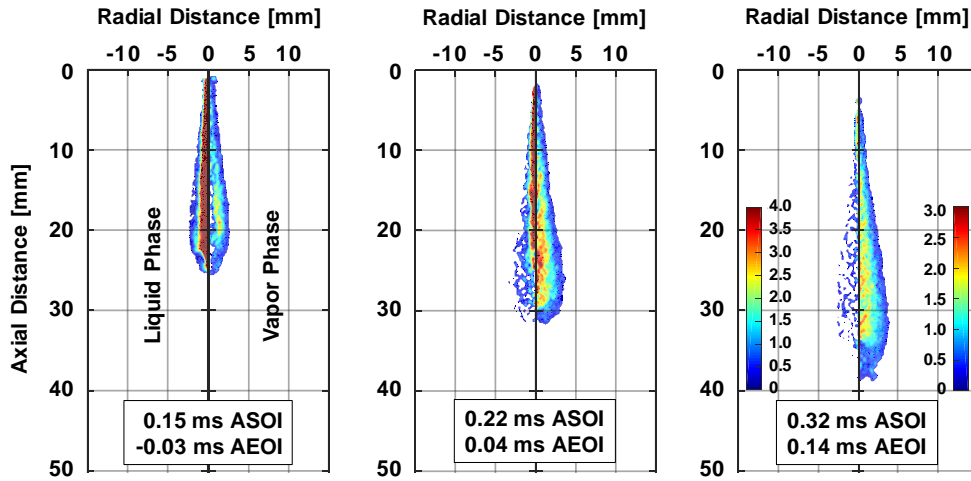
227 following of this article will mainly focus on the equivalence ratio of SH and MH

228 injectors.

229 Figures 8 and 9 show the spray equivalence ratio distributions for the two injectors

230 under same rail pressure and similar injection rate conditions, respectively. The right

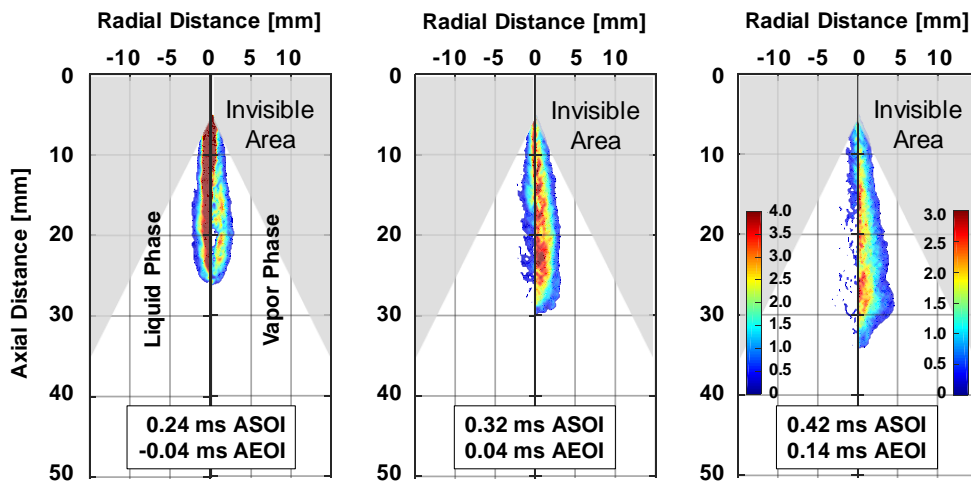
231 side of each spray picture represents the vapor phase and the other side is the liquid
232 phase. As described in Figure 2, the spray of MH injector has an invisible area near
233 the nozzle tip. As for the same rail pressure condition, the equivalence ratio
234 distribution of spray for SH and MH injectors shows a similar tendency versus time
235 when the end of injection (EOI) is set as time zero, no matter the moment is after the
236 end of injection (AEOI) or before the end of injection. However, for the similar
237 injection rate condition, a completely different scenario is presented. The spray of
238 the MH injector has a large amount of mass evaporated (the red spray center) before
239 the end of injection, while that of the SH injector still has a very high liquid
240 concentration at 0.05ms AEOI around the spray center. The spray equivalence ratio of
241 MH injector has become very low due to more gas entrainment and vapor diffusion
242 at 0.20ms AEOI. However, the spray center of SH injector (vapor phase) is still red
243 (high concentration and equivalence ratio), and even a small amount of liquid fuel
244 exists. In other words, the time required to form a homogeneous mixture is a very
245 noteworthy issue when the mixture formation of an SH injector is analogous to a MH
246 injector.



247

248

(a) Single-hole injector



249

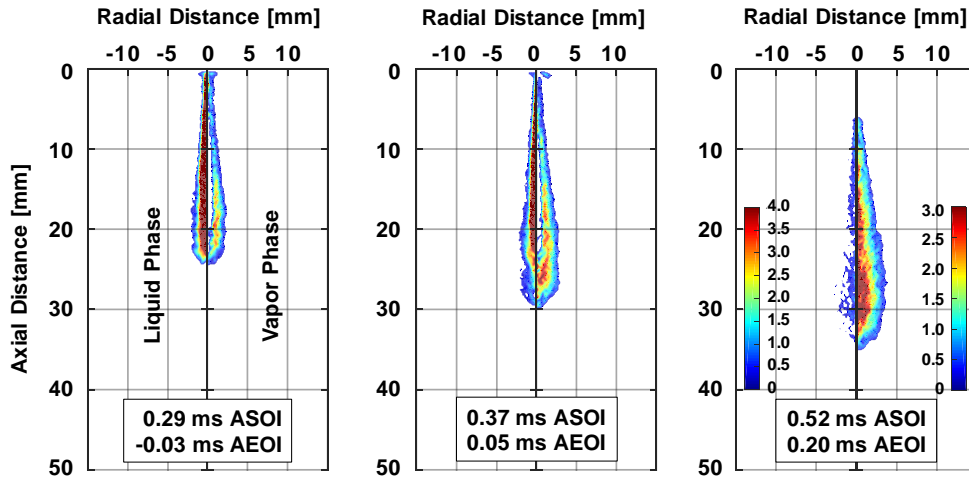
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(b) Multi-hole injector

251

Figure 8 Equivalence ratio distribution under same rail pressure of 100 MPa.

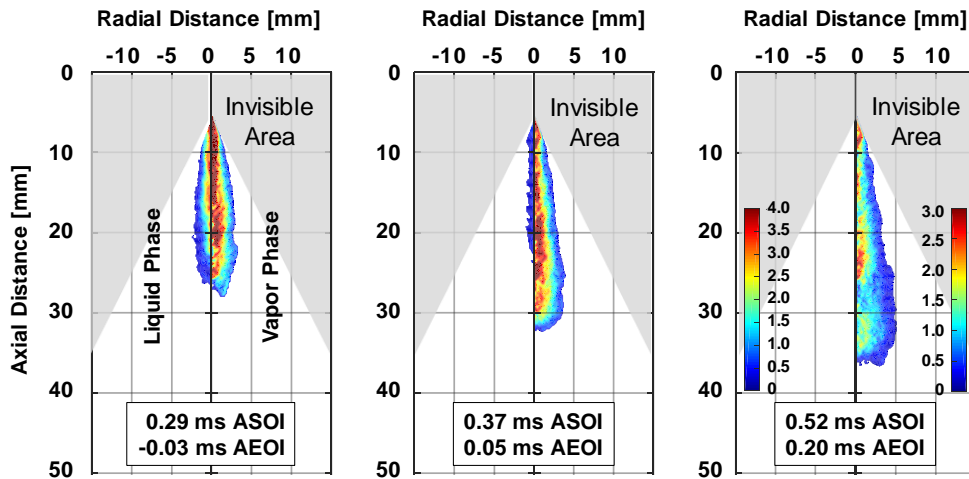
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253

254

(a) Single-hole injector



255

256

(b) Multi-hole injector

257

Figure 9 Equivalence ratio distribution under similar injection rate profile.

258

The three-dimensional average was performed for the equivalence ratio distributions,

259

and the variation curves of the spatial average (mean equivalence ratio) over time

260

were obtained as shown in Figure 10. The mean equivalence ratio peaks of both SH

261

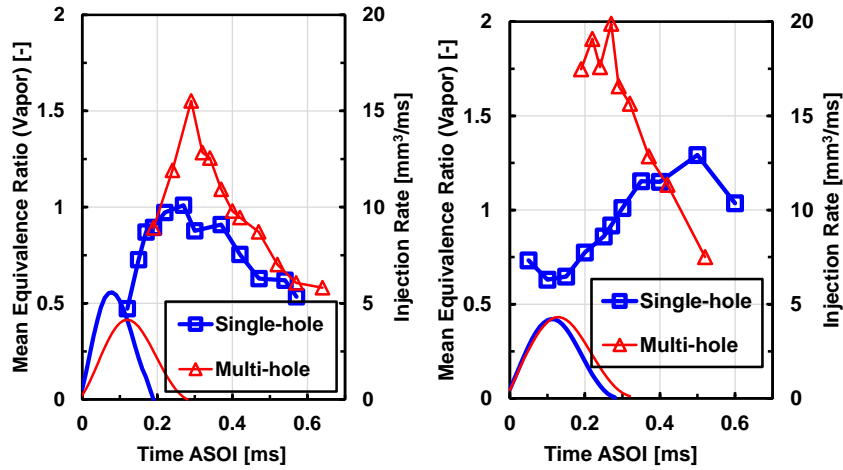
and MH injectors seem to appear near the end of injection under same rail pressure

262

condition, but the peak of SH injector appears to occur slightly later than the end of

263 injection. That means the equilibrium between air entrainment and fuel evaporation
264 occurs near the end of injection. Besides, we noticed that the mean equivalence ratio
265 of the MH injector is much larger than that of the SH injector. This should be due to
266 the faster evaporation rate or lesser air entrainment of the MH injector. We will
267 further explore the reasons when discussing the evaporation rate.

268 As for similar injection rate condition, the peak of mean equivalence ratio for the SH
269 injector obviously appears very late, about 0.2 ms AEOI (0.5 ms ASOI), where that of
270 MH injector has dropped to an extra low level. That reveals the spray of SH injector
271 has a quite low evaporation rate during the injection period. To illuminate this result,
272 we pulled out the mass of vapor production and entrained ambient gas under similar
273 injection rate condition (Figure 11). Obviously, the vapor production of MH injector is
274 more than twice of SH injector before the end of injection, even though the disparity
275 of entrained ambient gas has no such large gap. There must be other factors that
276 make a big difference in the atomization process. It shows that the influence of
277 internal flow of nozzle on its atomization cannot be underestimated.



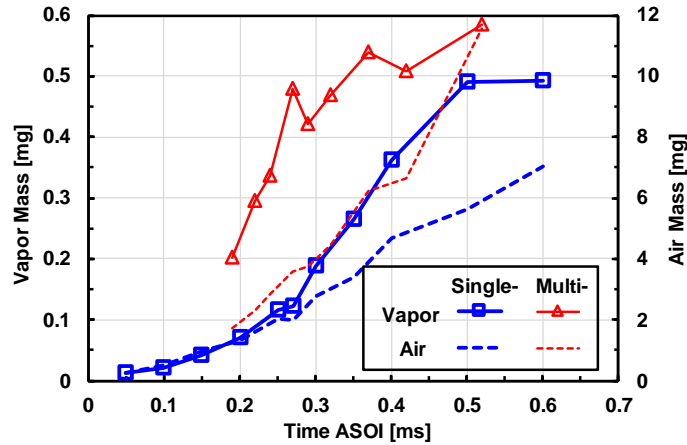
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279

(a) Same rail pressure of 100MPa (b) Similar injection rate

280

Figure 10 Mean equivalence ratio.



281

282 Figure 11 Vapor production and entrained ambient gas under similar injection rate

283

condition.

284 Figure 12 shows the evaporation ratio versus time which is based on ASOI for the

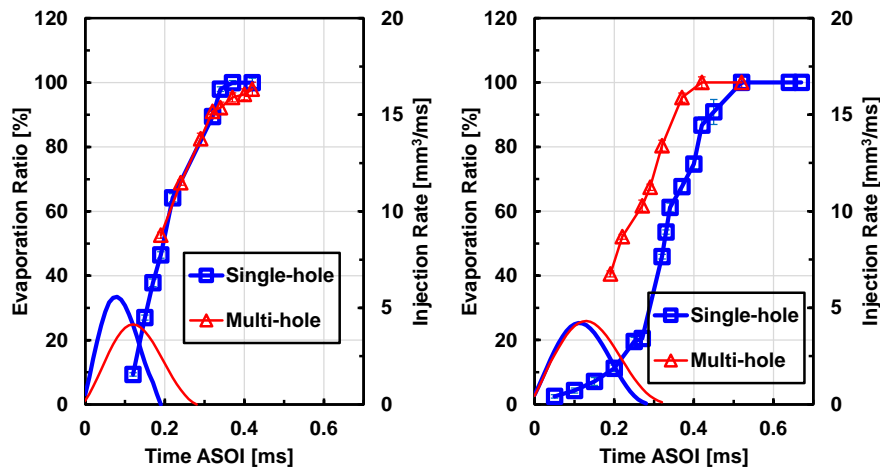
285 sprays of the two injectors. As for the same rail pressure condition showed in Figure

286 12(a), the evaporation ratio of SH and MH injectors show a similar trend. Therefore,

287 the evaporation ratio is not the reason why the MH injector has a larger equivalence

288 ratio which was discussed in Figure 10. Then there is only one crucial reason (less

289 entrained gas mass) left for the larger equivalence ratio of MH injector. That is to say,
 290 although the spray angle of MH injector is larger, the longer spray tip penetration of
 291 the SH spray can make up for the loss in mixture volume caused by small spray angle.
 292 As for similar injection rate condition, the spray of SH injector shows a quite slower
 293 evaporation ratio comparing with that of MH injector. The spray angle (or spray
 294 volume) is one of the most important reasons for that. In addition, as mentioned
 295 above, the effect of nozzle flow on the atomization process is also very important.

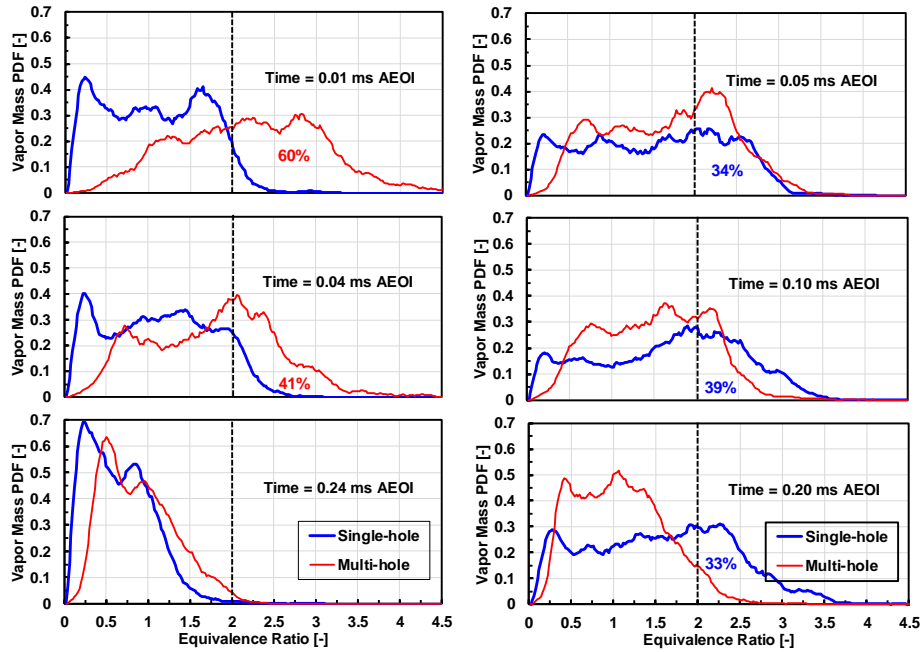


296 (a) Same rail pressure of 100MPa (b) Similar injection rate

297 Figure 12 Evaporation ratio.

299 All in all, our ultimate goal is to form a high-quality mixture to improve combustion
 300 efficiency and reduce emissions. The relationship between mixture concentration
 301 (equivalence ratio) and time (crank angle) is extremely important, which will to a
 302 large extent affect the heat release rate of combustion and indicated efficiency.
 303 Hence, the vapor mass distribution versus equivalence ratio at different instants

304 should be considered very circumspect. As shown in Figure 13 (a), most fuel vapor of
305 SH injector is distributed in the region where the equivalence ratio is less than 2 after
306 the end of injection. However, 60% of the fuel vapor in MH injector is located in the
307 region where the equivalence ratio larger than 2 at the end of injection and
308 dispersed to the low concentration region rapidly. Although the tendency of vapor
309 concentration looks absolutely different for two injectors, the region with high vapor
310 concentration of MH injector quickly disappeared, which may have little effect on
311 soot emission in the combustion process. Further combustion experiment is required
312 to get the final conclusion. As for the similar injection rate condition, there is no
313 doubt that the vapor mass distribution of MH injector shows the same scene with
314 the same rail pressure condition. In contrast, the spray of SH injector still has more
315 than 30% vapor distributed in the high concentration region (equivalence ratio
316 greater than 2) 0.20 ms AEOI. The slower evaporation rate is one of the reasons.
317 Nevertheless, lower dispersion rate, caused by the lower turbulence kinetic energy
318 and lower radial velocity, should be a more influential factor, which will be discussed
319 later.



320

321

(a) Same rail pressure of 100MPa (b) Similar injection rate

322

Figure 13 Vapor mass distribution with equivalence ratio.

323

3.2 Nozzle flow and near-field spray in CFD simulation results

324

As discussed above, the nozzle internal flow plays a crucial role in spray and mixture

325

process, and indirectly affects the combustion process and emissions. In order to

326

better interpret the phenomena found in the experiment section, the internal and

327

near-field flow simulation of the SH and MH nozzles has been conducted for similar

328

injection rate condition. Figure 14 shows the needle lift curves used in nozzle flow

329

simulation and the flow rate comparison between simulation and experiment. The

330

needle lift curves were simplified from the X-Ray data of AIST (Advanced Industrial

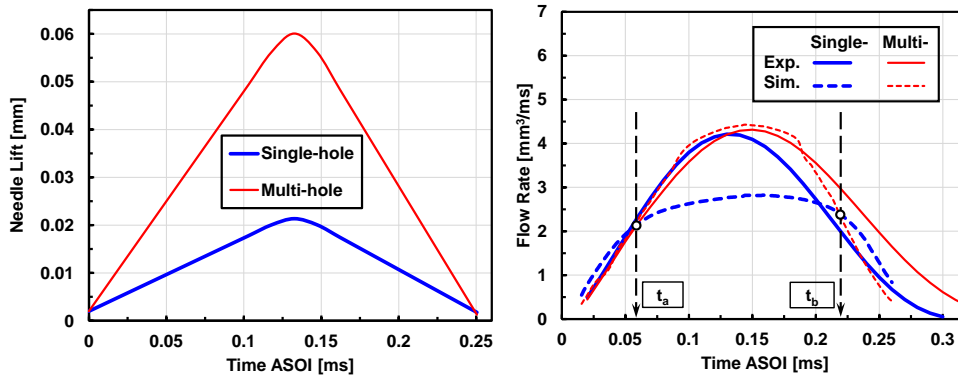
331

Science and Technology) which used the same type of injectors as well as the authors.

332

Two moments (t_a and t_b) of flow rate curves were selected for subsequent discussion

333 on flow characteristic under both needle rising and falling processes.



334

335

(a) Needle lift curve (b) Flow rate comparison with simulation

336

Figure 14 Needle lift in simulation and flow rate comparison.

337

To comprehend the content of following figures easily, Figure 15 shows the X, Y, Z

338

coordinates at hole exit. The center of hole exit was selected as the origin of

339

coordinates. The radial velocity magnitude and turbulence kinetic energy (TKE) at

340

hole exit and 1mm downstream ($Z = 1$ mm) will be discussed in Figures 17, 18 and 19.

341

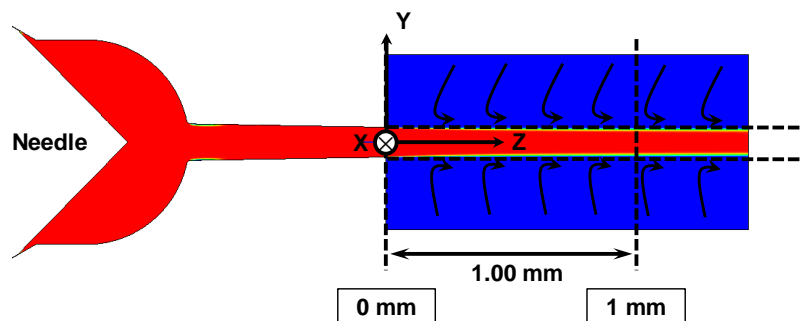
The radial velocity is defined as vector sum of velocity compositions in X and Y

342

directions, as shown in Eq. (5). The distance between the dashed lines shown in the

343

figure is 0.125mm (hole diameter).



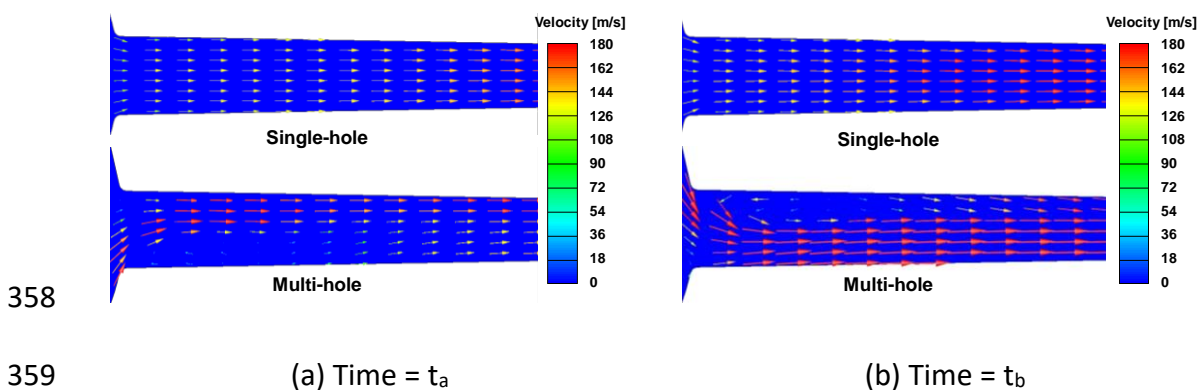
344

345

Figure 15 X, Y, Z coordinates at hole exit

346
$$\vec{v}_r = \vec{v}_x + \vec{v}_y \tag{5}$$

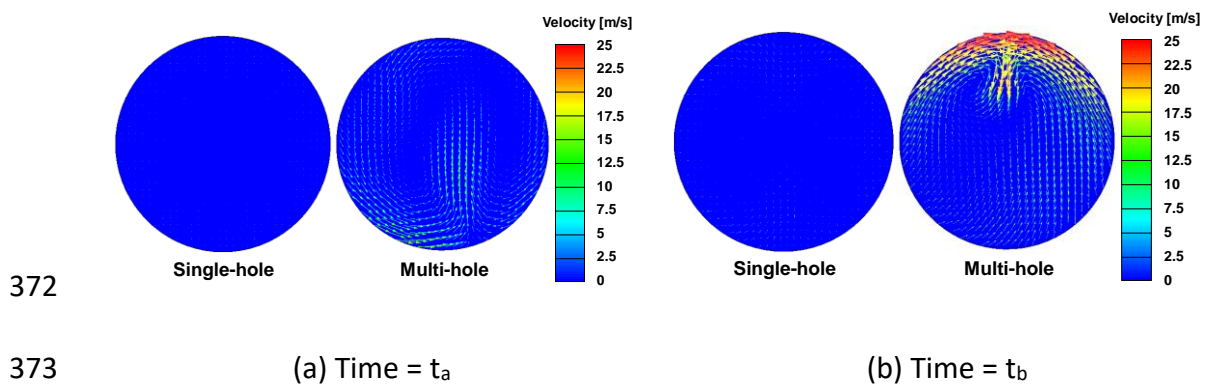
347 Figure 16 shows the velocity vectors of longitudinal section along the holes. It is
 348 obviously that, no matter hole exit or other cross sections, both the vector direction
 349 and velocity magnitude inside the hole of SH nozzle are extremely uniform along the
 350 cross section (Y coordinate). Totally different from the SH nozzle, the velocity vectors
 351 have various features along both the hole axis (Z coordinate) and radial direction.
 352 This fascinating sight is even more evident in the radial velocity distributions at the
 353 hole exit (Figure 17). The sharp change in velocity direction of the hole is mainly
 354 caused by the backflow formed by the fluid entering the hole, which also leads to an
 355 inconformity in velocity magnitude of hole exit. This unique characteristic of MH
 356 nozzle can significantly increase the radial velocity of the spray, thereby promoting
 357 subsequent atomization and air entrainment.



360 Figure 16 Velocity distributions inside holes

361 The radial velocity vectors of SH and MH nozzles at the hole exit are shown in Figure

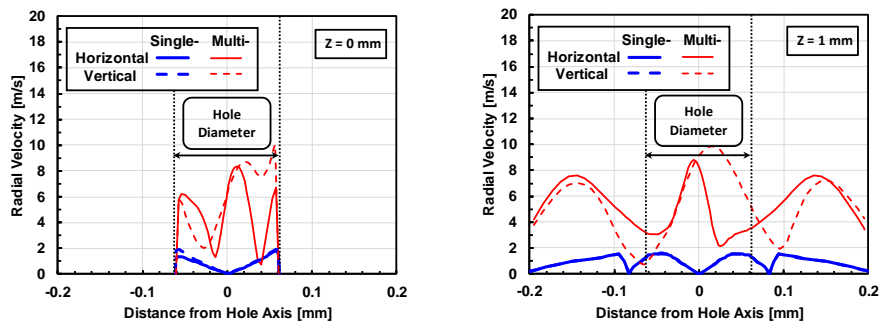
362 17. The radial velocity of MH exit is obviously higher than that of the SH during either
 363 the needle rising or falling period. Besides, two large vortexes occur inside the hole
 364 of MH nozzle, which were caused by the elbow-like structure, and will increase the
 365 TKE magnitude, improve the atomization process and enhance air entrainment. It is
 366 worth noting that the radial velocity peak of MH exit at t_b is significantly greater than
 367 that of t_a , even it shows the similar flow rate at the two moments in Figure 14(b). We
 368 all know that the total evaporation time should be connected with fuel injected at
 369 the moments near the end of injection. That is to say, for the MH injector, the large
 370 radial velocity at hole exit near the end of injection is an important reason for the
 371 faster evaporation rate.



374 Figure 17 Radial velocity distributions at hole exit

375 Figures 18 and 19 show the radial velocity and TKE magnitude along the horizontal
 376 and vertical lines at both the hole exit ($Z = 0$ mm) and 1 mm downstream ($Z = 1$ mm).
 377 As for MH injector, the horizontal line is defined base on the placement shown in

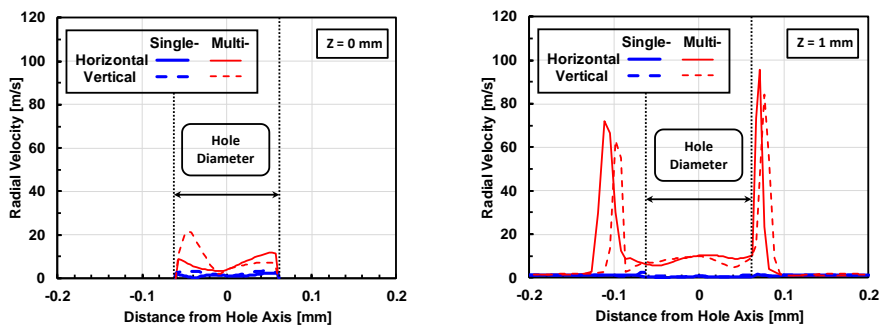
378 Figure 3. The radial velocity and TKE of air region which represent the air
 379 entrainment at $Z = 1\text{ mm}$ are also shown in the figures. Overall, no matter the radial
 380 velocity or TKE magnitude, the values of MH are much larger than that of SH at both
 381 hole exit and downstream. What is worth mentioning is that the large values in (or
 382 near) the hole axis of MH can great enhance the atomization process by promoting
 383 the liquid core breakup.



384

385

(a) Time = t_a



386

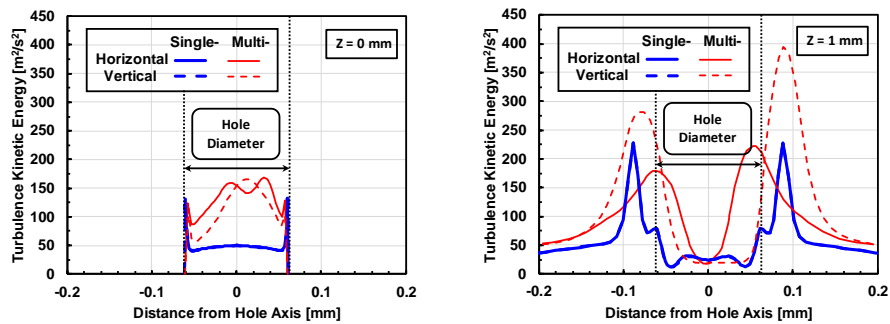
387

(b) Time = t_b

388 Figure 18 Radial velocity magnitude distributions along the horizontal (X) and vertical
 389 (Y) lines at $Z = 0\text{ mm}$ and $Z = 1\text{ mm}$.

390 As mentioned before, the MH injector has a large spray angle under both the same

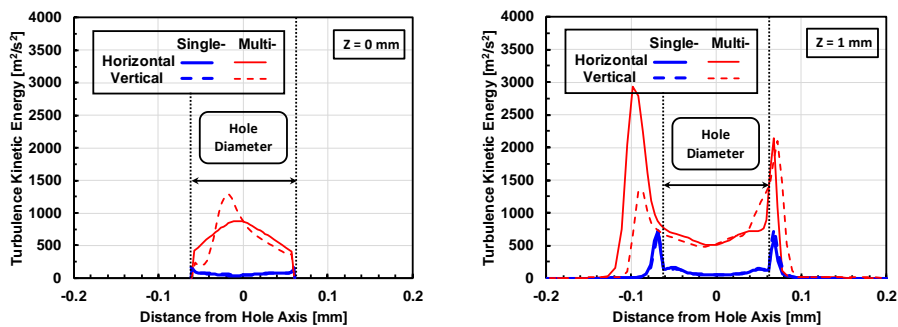
391 rail pressure and similar injection rate conditions. The larger radial velocity and TKE
 392 must make a lot of contributions to spray angle. That is why the evaporation rate of
 393 MH injector can catch up with that of the SH injector under the same injection
 394 pressure. In addition, the evaporation rate of MH spray is much faster than that of SH
 395 under similar injection rate condition, which is closely related to the radial velocity
 396 and TKE of hole exit. That is beneficial to the formation of homogeneous mixtures,
 397 both spatially and temporally.



398

399

(a) Time = t_a



400

401

(b) Time = t_b

402 Figure 19 Turbulence kinetic energy distributions along the horizontal (X) and vertical

403

(Y) lines at Z = 0 mm and Z = 1 mm.

404 **Conclusions**

405 A comparison on the mixture formation process of a fuel spray between single-hole
406 (SH) and multi-hole (MH) injectors has been conducted. The laser absorption
407 scattering (LAS) technic was performed to obtain the fuel equivalence ratio
408 distributions of vapor and liquid phases. A blended fuel of α -MN and n-tridecane was
409 used in the experiment. The spray evolution with small injection amount under same
410 injection pressure (100 MPa for both injectors) or similar injection rate condition (30
411 MPa for SH injector, and 100 MPa for MH injector) were observed, respectively.
412 Following conclusions can be made accordingly.

413 1. Under the same injection pressure condition, the vapor penetration of SH injector
414 is greater than that of MH injector, due to the faster sac pressure build-up process.

415 2. MH injector has a larger spray angle than SH injector caused by the complex
416 internal flow. The results of nozzle flow simulation show that there were greater
417 portion of radial velocity term at the nozzle exit of MH injector at the transient
418 period (low needle lift condition). This might have yielded a high spray angle for MH
419 injector with small injection quantity, either under the same rail pressure or similar
420 injection rate conditions.

421 3. The mixture formation of SH injector is slightly better than that of MH injector
422 under same injection rate condition. The entire injection event of small injection

423 amount took place under the transient condition. The greater spray tip penetration
424 caused by the faster sac pressure build-up process yielded greater air entrainment
425 rate and amount for the SH injector. However, the difference in air entrainment rate
426 and amount as a function of axial distance can be eliminated for both injectors under
427 the same injection rate condition, since their vapor penetrations are similar to each
428 other. The mixture formation process for SH injector then become worse than that of
429 MH injector. The narrow spray angle and dense liquid core of the SH injector caused
430 a lower evaporation ratio at the EOI timing. The overall equivalence ratio moves
431 towards lean side for the MH injector as the time elapsed. However, since the SH
432 injector no longer has any advantages on the vapor penetration, the evaporation rate
433 is slow, and the mixture is not able to lean out quickly due to continuous portion of
434 liquid core evaporating into vapor, maintaining the rich mixture. The mixture starts to
435 lean out after when the vapor was fully evaporated.

436 4. Regarding the same injection pressure condition, the vapor penetration plays an
437 important role in the evaporation rate and air entrainment, thus improved the lean
438 mixture formation process, despite of the smaller spray angle of SH injector has.
439 When the vapor penetration becomes similar (by means of controlling the injection
440 pressure) for both injectors, the mixture formation becomes worse for SH injector as
441 a result of the smaller spray angle and dense liquid core.

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446

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