Unconventional Superconductivity in Electron-Doped Layered Li_{0.48}(THF)_yHfNCl

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We report magnetic susceptibility measurements on a layered superconductor $\text{Li}_{0.48}(\text{THF})_{0.3}\text{HfNCl}$ having $T_c \sim 26$ K. The present study revealed that (a) the Fermi level density of states is small, $N^*(E_F) \sim 0.25$ states/(eV spin f.u.), (b) mass enhancement is negligible, $\tilde{\gamma} \sim 1$, (c) electron-phonon coupling is weak, $\lambda_{ep} \ll 1$, (d) exchange enhancement is negligible, $1/(1 + F_0^a) \sim 1$, and (e) electronic density parameter is large, $r_s^{2D} \sim 10.3$ (i.e., low-carrier density). It is difficult to explain the origin of the high T_c in terms of the conventional phonon (BCS) mechanism of superconductivity.

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In 1998, Yamanaka and co-workers discovered a new layered superconductor $\text{Li}_x(\text{THF})_y\text{HfNCl}$ (THF; tetrahydrofuran C₄H₈O) with $T_c \sim 26$ K [1]. The mother compound β -HfNCl is a semiconductor with a band gap of \sim 4 eV having layered structure stacking the Cl-[HfN]-[NHf]-Cl slabs along the *c* axis [1,2]. As shown in Fig. 1(a), Li atoms are cointercalated with THF molecules into the weak van der Waals gap between the Cl layers and the interlayer distance *d* increases from 9.23 Å in β -HfNCl to 18.7 Å in Li_{0.48}(THF)_{0.3}HfNCl (Li-HfNCl) [1]. On intercalation, electrons are doped into the (HfN)₂ layer and the system shows superconductivity with a relatively high T_c of ~26 K [1].

Experimental and theoretical studies have clarified the variety of physical properties, as follows: (1) T_c of ~26 K exceeds 23 K of a conventional BCS superconductor, Nb₃Ge [3]. A question as to why such a high T_c is realized naturally arises. (2) Bulk superconductivity suddenly appears with $T_c \sim 26$ K at the doping content of $x \sim 0.13$. T_c is almost constant (~26 K) up to $x \sim 0.5$ but gradually decreases to $T_c \sim 24.4$ K with further doping [1], suggesting a low-carrier-density system. (3) Band calculations revealed a two-dimensional (2D) electronic structure originating in planer Hf- d_{xy} , $d_{x^2-y^2}$ orbitals strongly hybridized with N- p_x , p_y orbitals having broad bandwidths of $w \sim 1.5$ eV, suggesting a weakly correlated electron system [4-6]. (4) Actually, we reported the quasi-2D superconducting (SC) properties in Li-HfNCl from dc-magnetization and NMR measurements for c-axis oriented pellets [7]. (5) An exotic SC nature near the Bose-Einstein condensation limit was reported from muon spin relaxation measurements [8].

In the present work, the magnetic susceptibility measurements of the *c*-axis oriented Li-HfNCl pellets were carried out in the temperature (*T*) range of 4–300 K for magnetic fields applied parallel to the *ab* plane ($H \parallel ab$) and the *c* axis ($H \parallel c$). From analyses of the present data together with the previous results [7], we clarify the unsuccessful explanation of T_c within a traditional BCS framework.

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Detailed sample preparation techniques for the powder Li-HfNCl sample were reported in Ref. [1]. The powder sample was compressed into a pellet of 4 mm in diameter and 0.5 mm in thickness under a pressure of 1.5 kbar in argon atmosphere. The sample was roughly cut into disks of ~ 2 mm in diameter and sealed in a quartz tube with helium gas at 350 torr [7]. X-ray locking curve measurements revealed that the c axis was aligned in a Gaussian distribution with a half-width of less than 3.5° in the pellet. We prepared two oriented pellets (No. 1 and No. 2). Sample No. 1 is the same batch as in the previous paper [7]. The static magnetic susceptibility was measured using a commercial SQUID magnetometer (MPMS, Quantum Design). In order to subtract the diamagnetism of the quartz tube, the susceptibility of the sample was obtained from subtraction between two measurements for the tube containing the sample and the "empty" tube itself.

In Fig. 1(b), we show the dc-magnetic susceptibility data (No. 1) of Li-HfNCl for the zero-field cooling protocol, where the Meissner shielding occurs at $T_c = 25.56$ K. An evident difference in susceptibilities for $H \parallel ab$ and



FIG. 1. (a) Schematic structural model and (b) dc-magnetic susceptibility of $\text{Li}_{0.48}(\text{THF})_{0.3}\text{HfNCl}$ with field (H = 5 Oe) parallel to the *c* axis $(H \parallel c)$ and to the *ab* plane $(H \parallel ab)$. Arrow shows $T_c (= 25.56 \text{ K})$ for H = 5 Oe.

H || *c* reflects the anisotropic nature of the SC state due to the layered structure [7]. The volume fraction of the SC state for *H* || *c* at 4 K is ~95% (~78% for No. 2) of the theoretical value $-1/4\pi$. Here, the correction on the demagnetizing field was performed assuming the disk.

The *T* dependence of susceptibility (χ_0) of Li-HfNCl (No. 1) for *H* || *ab* and *H* || *c* is shown in Fig. 2. A typical magnetization curve of Li-HfNCl (No. 1) for *H* || *ab* is shown in the inset. A ferromagnetic background corresponds to ~150 ppm spins per formula unit (f.u.) independent of field direction, which should be due to impurity domains. Therefore we determined χ_0 from the difference between the values at *H* = 40 and 20 kOe in order to subtract the ferromagnetic background. For sample No. 2, χ_0 agrees with that for No. 1 within the accuracy of $\pm 2 \times 10^{-6}$ emu/mol. The susceptibility of β -HfNCl is also shown, represented by a dashed line, which gives a Curie tail corresponding to 0.15% spins/f.u.

A negative value of χ_0 implies that the Pauli susceptibility χ_s is of the order of the diamagnetic susceptibility χ_{dia} . Actually, the Pauli susceptibility becomes $\chi_s(T_c) \sim 1.7 \times 10^{-5}$ emu/mol at T_c , which is about one-tenth of that of conventional BCS superconductors, by subtracting the diamagnetism; $\chi_s = \chi_0^i - \chi_{\text{core}} - \chi_L^i - \chi_{\text{orb}}^i$ (i = ab and c), where χ_{core} , χ_L^i , and χ_{orb}^i are the core diamagnetic susceptibility, Landau diamagnetism, and orbital susceptibility, respectively. χ_{core} is estimated from the increments of values, $\chi_{\text{Li}^+}^{\text{core}} \sim -6.0 \times 10^{-7}$ emu/mol, $\chi_{\text{HfNC1}}^{\text{core}} \sim -3.4 \times 10^{-5}$ emu/mol (estimated from the T-independent part of the pristine HfNC1), and $\chi_{\text{THF}}^{\text{core}} = -1.57 \times 10^{-5}$ (y = 0.3) emu/mol (calculated by the Pascal's method for organic molecules [9]). χ_L is given



FIG. 2. Temperature dependence of susceptibility of $Li_{0.48}$ -(THF)_{0.3}HfNCl for $H \parallel c$ (circles) and $H \parallel ab$ (triangles). The dashed curve is the susceptibility of β -HfNCl. The procedure of the decomposition of the parameters is given in the text. The inset gives the magnetization curve for $H \parallel ab$ at T = 300 K.

by $-(m/m^*)\chi_s/3$, where *m* is the free electron mass and m^* is the effective mass. Because the mass anisotropy is very large $\Gamma \sim 14$ [7], χ_L would be negligible for $H \parallel ab$, whereas $-\chi_s/3$ for $H \parallel c$. χ_{orb}^{ab} and χ_{orb}^{c} are estimated to be -10^{-6} and 0 emu/mol, respectively, using the prescription by Clogston *et al.* [10].

Now, we discuss the electronic properties within the Fermi liquid model [11], where the mass *m* is enhanced by $\tilde{\gamma} = m^*/m$ as a result of the electron-electron interaction. The renormalized Fermi level density of states $N^*(E_F) = N(E_F)\tilde{\gamma}$ can be estimated from the following relationship: $\chi_s = 2N_A \mu_B^2 N^*(E_F)/(1 + F_0^a)$, where $N(E_F)$ is the bare density of states and F_0^a is the Landau parameter. The obtained value for χ_s gives us $N^*(E_F)/(1 + F_0^a) \sim 0.26$ states/(eV spin f.u.).

Alternatively, we can estimate $N^*(E_F)$ from the thermodynamics in the SC state; $H_c(0)^2 V_{\text{mol}}/(8\pi) = (F_n - F_s)_{T=0} \sim (1 + \lambda_{ep})N^*(E_F)\Delta^2/2$ with $V_{\text{mol}} = 59.93 \text{ cm}^3/\text{mol}$, where F_n and F_s are the free energy in the normal and SC states, respectively, and λ_{ep} is an electron-phonon coupling constant. Assuming the weak-coupling value of $2\Delta = 3.53k_BT_c$, and using $H_c(0) = 845 \text{ Oe}$ [7], the effective density of states is calculated to be $(1 + \lambda_{ep})N^*(E_F) \sim 0.24$ states/(eV spin f.u.), where k_B is the Boltzmann factor. Correspondingly, the electronic specific heat coefficient γ_{el} is calculated to be 1.1 mJ/ (mol K²) from $\gamma_{el} = (1 + \lambda_{ep})(2/3)\pi^2k_B^2N^*(E_F)$.

These values are comparable to $N(E_F) \sim 0.19-0.26$ states/(eV spin f.u.) obtained from the band calculations [4–6]. Thus, $\tilde{\gamma}/(1 + F_0^a) \sim 1$ and $\tilde{\gamma}(1 + \lambda_{ep}) \sim 1$, implying negligible mass enhancement, $\tilde{\gamma} \sim 1$, weak electronphonon coupling, $\lambda_{ep} \ll 1$ [12], and negligible exchange enhancement, $1/(1 + F_0^a) \sim 1$. These are consistent with the theoretical prediction, i.e., weak electronic correlation and weak electron-phonon coupling, by Weht *et al.* [6].

The obtained $N(E_F)$ is also very close to that of a 2D free electron gas model: $N^{2D}(E_F) = mS_{mol}/2\pi\hbar^2 \sim$ 0.23 states/eV with $S_{\rm mol} = 6.67 \times 10^8 \text{ cm}^2/\text{mol}$, where \hbar is the Planck constant. Together with the quasi-2D SC properties [7], the electronic state of Li-HfNCl may be approximately described in terms of a 2D electron gas model. The characteristic parameters in the 2D electron gas model [13] are listed in Table I. Here, the Fermi wave number k_F was estimated using the relations $\xi_0 \sim$ $\hbar^2 k_F / (m^* \pi \Delta) \sim 1.35 \xi_{\rm GL}$ in the clean limit BCS superconductor [7] and the specific heat coefficient for the 2D case $\gamma_{el}^{2D} = \pi k_B^2 m^* S_{mol} / (3\hbar^2)$, where $\xi_{GL} = \xi_{ab} \sim$ 60 Å [7] and ξ_0 are the Ginzburg-Landau and BCS coherence lengths, respectively. Those for the 3D model, those of Nb, Ba_{0.6}K_{0.4}BiO₃ (BKBO) [14], and YBa₂Cu₃O₇ (YBCO) [15] were also calculated as references. The obtained value, $k_F \sim 1.3 \times 10^7 (\sim 1.6 \times 10^7 \text{ for the 3D case})$ cm^{-1} , for the simple electron gas model is consistent in order of magnitude with the theoretical value of 1.95 \times 10^7 cm^{-1} [6], suggesting that the model is applicable to the present system. We note that the estimated SC carrier

TABLE I. Characteristic parameters of Li-HfNCl obtained from the experiments and derived from the electron gas model [13], assuming $\langle \omega_{ph} \rangle = 300$ K. n_s for the 2D case is obtained as n_s^{2D}/d (d = 18.7 Å; the interlayer distance). Those for the 3D case were calculated using $\xi_{GL} = (\xi_{ab}^2 \xi_c)^{1/3} \sim 38$ Å. As references, the parameters of Nb, BKBO, and YBCO have also been calculated assuming the 3D electron gas model [13]. The parameters used here are as follows: Nb: $2\Delta = 3.8k_BT_c$, $\xi_0 = 390$ Å, and $\langle \omega_{ph} \rangle = 166$ K; BKBO (dirty limit): $\gamma_{el} = 2$ mJ/mol K², $2\Delta = 4k_BT_c$, $\xi_0 = 1.83\xi_{GL}^2/l \sim 89$ Å, $\xi_{GL} \sim 40$ Å, $l \sim$ 33 Å, $\langle \omega_{ph} \rangle \sim 550$ K [14]; YBCO: $\gamma_{el} \sim 40$ mJ/mol K², $2\Delta/k_BT_c \sim 6$, and $\xi_{GL} = (\xi_{ab}^2 \xi_c)^{1/3} \sim 7$ Å [15].

Parameters	Li-HfNCl		Nb	BKBO	YBCO
T_c (K)	25.5		9.3	30	92
$\gamma_{\rm el} ({\rm mJ}/{\rm mol}{\rm K}^2)$	1.1		7.8	~ 2	~ 40
$N(E_F)$ (states/eV)	0.25		0.5	~0.3	~3
Model	2D	3D	3D	3D	3D
T_F (K)	735	596	18 400	3430	3350
$k_F \ (10^7 \ {\rm cm}^{-1})$	1.29	1.63	17.9	3.95	8.23
$n_s (10^{20} \text{ cm}^{-3})$	1.42	2.19	1940	20.9	190
r_s	10.3	22.3	2.0	13.8	(44)
$k_{\rm TF}~(10^7~{\rm cm}^{-1})$	37.8	6.3	20.8	11.95	(44.5)
μ^{*}	(0.35)	(0.34)	0.11	0.23	
λ_{ep}	(2.42)	(2.38)	0.91	1.3	

density n_s is quite low ~1.4 × 10²⁰ cm⁻³ in comparison with the value calculated from the valency, similarly to the case for the organic superconductor (BEDT-TTF)₂-X [16]. Corresponding to the low-carrier density, T_F^{2D} ~ 735 K is also relatively low, which is in good agreement with the value of $T_F^{2D} = 987$ K obtained by μ SR measurement [8].

The remarkable findings in the present studies are summarized as follows: (a) the Fermi level density of states is small, $N(E_F) \sim 0.25$ states/(eV spin f.u.), (b) the mass enhancement is negligible, $\tilde{\gamma} \sim 1$, (c) the electron-phonon coupling is weak, $\lambda_{ep} \ll 1$, (d) the exchange enhancement is negligible, $1/(1 + F_0^a) \sim 1$, and (e) the electronic density parameter is large, $r_s^{\rm 2D} \sim 10.3$ (i.e., low-carrier density).

Why is such a high T_c realized in this system? In conventional BCS superconductors with high-carrier density $\sim 10^{23}$ cm⁻³, we have the versatile prescription for T_c given by McMillan and Allen and Dynes [17]:

$$T_c = \frac{\langle \omega_{ph} \rangle}{1.2} \exp \frac{-1.04(1+\lambda_{ep})}{\lambda_{ep} - \mu^*(1+0.62\lambda_{ep})}, \quad (1)$$

where $\langle \omega_{ph} \rangle$ and μ^* are the typical phonon energy and the Coulomb pseudopotential, respectively. This equation can be applied when the screening is sufficient to disregard the long-range Coulomb interaction and the Morel-Anderson model well describes retardation effects of the screened short-range Coulomb interaction [18]:

$$\mu^* = \mu / [1 + \mu \ln(\omega_{el} / \langle \omega_{ph} \rangle)], \qquad (2)$$

with the typical screened Coulomb potential $\mu = (a^2/2) \ln[(1 + a^2)/a^2]$, where $a^2 = k_{TF}^2/(4k_F^2)$, k_{TF} is

the Thomas-Fermi wave number. ω_{el} is the typical electron energy scale, e.g., the Fermi energy E_F or the plasma frequency ω_{pl} for a single band metal. In usual metals, it gives $\mu^* \sim 0.1-0.13$.

Since $\tilde{\gamma} \sim 1$ and $1/(1 + F_0^a) \sim 1$ for the present case, μ^* is expected to be small. If we assume $\mu^* = 0.1$ and $\langle \omega_{ph} \rangle = 300$ K, then we have $\lambda_{ep} \sim 1.17$ in a region of strong coupling limit by using Eq. (1). Alternatively, we can directly estimate μ^* by using Eq. (2). In the single band model, μ^* is calculated to be ~0.35 using the values listed in Table I. Then λ_{ep} turns out to be significantly large, $\lambda_{ep} \sim 2.42$ [19]. These are inconsistent with both the present result and the theoretical prediction [6], i.e., $\lambda_{ep} \ll 1$. Even if $\lambda_{ep} > 1.17$ is valid, the electron-phonon interaction $V_{ep} \sim \lambda_{ep}/N^*(E_F) > 4.7$ eV, which is much larger than the bandwidth $w \sim 1.5 \text{ eV}$ [4–6], would be too strong to realize the conventional BCS superconductivity, and instead may lead to lattice instability. Finally, we can assume $\mu^* = 0$, but even then the observed T_c cannot be attributed solely to the higher frequency modes, e.g., $\langle\omega\rangle_{ph}\sim$ 850 K by nitrogen motion, as discussed by Weht et al. [6]. Anyhow, it seems to be quite difficult to explain the observed T_c within the framework of the conventional BCS mechanism.

Turning our attention to the relation $2k_F/k_{\rm TF} < 1$ in Li-HfNCl, we expect that the screening effect is significantly different from that in usual metals. Unless the dielectric screening is sufficient ($\epsilon > 12$ for 2D case), the long-range Coulomb interaction should not be ignored. In this context, the McMillan-Allen-Dynes relation as well as the Morel-Anderson model probably cannot be applied anymore. What mechanism can be realized in this system?

A spin-fluctuation mechanism of superconductivity discussed in the strongly correlated electron system may be excluded because of no evidence for the strong electronic correlation, e.g., negligible mass enhancement $\tilde{\gamma} \sim 1$ and/or broad bandwidth of $w \sim 1.5$ eV. Takada, and Rietschel and Sham predicted that the charge fluctuation due to long-range Coulomb interactions (i.e., plasmon) is possible to mediate high T_c superconductivity in a lowcarrier-density system when the electron-phonon coupling and short-range Coulomb interactions play a minor role [20]. In this case, both $\tilde{\gamma}$ and $1/(1 + F_0^a)$ are predicted to be of the order of unity. Our findings, (a)–(e), seem to meet the requirement for a charge-fluctuation mechanism of superconductivity [20].

Meanwhile, we note that the situation (the low-carrierdensity, small density of states, and high T_c) is somewhat similar to the case for BKBO [14]. Thus comparisons with the physical properties in BKBO may help in understanding the unconventional superconductivity in Li-HfNCl.

In summary, we have performed magnetic susceptibility experiments on the layered superconductor, $Li_{0.48}$ -(THF)_{0.3}HfNCl. These studies establish that Li-HfNCl is a low-carrier-density system. Taking account of the weak electron-phonon coupling and the small Fermi level den-

sity of states, it is difficult to explain the origin of the high T_c in terms of conventional electron-phonon coupling BCS superconductivity. Some other mechanisms beyond the conventional BCS theory should be sought as the origin of the high T_c in this system. A possible mechanism is a charge-fluctuation mechanism, although this may not be the only interpretation of our measurements. Thus the issue of why such a high T_c is realized, including the mechanism of superconductivity, remains an open question, and further detailed experimental and theoretical studies are required.

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- S. Yamanaka, K. Hotehama, and H. Kawaji, Nature (London) **392**, 580 (1998); S. Yamanaka, Annu. Rev. Mater. Sci. **30**, 53–82 (2000).
- [2] S. Shamoto *et al.*, Physica (Amsterdam) **306C**, 7 (1998);
 J. Phys. Chem. Solids **60**, 1431 (1999).
- [3] L. R. Testardi, J. H. Wernick, and W. A. Royer, Solid State Commun. 15, 1 (1974).
- [4] I. Hase and Y. Nishihara, Phys. Rev. B 60, 1573 (1999);
 Physica (Amsterdam) 281B-282B, 788 (2000).
- [5] C. Felser and R. Seshadri, J. Mater. Chem. 9, 459 (1999).
- [6] R. Weht, A. Filippetti, and W.E. Pickett, Europhys. Lett. 48, 320 (1999).
- [7] H. Tou et al., Phys. Rev. B 63, 020508(R) (2001).
- [8] Y. J. Uemura *et al.*, Physica (Amsterdam) **289B–290B**, 389 (2000); their estimate is based on the square lattice. For the triangular lattice, $T_F^{2D} = 938$ K is replaced by $T_F^{2D} = 731$ K.
- [9] Landolt-Börnstein, Numerical Data and Functional Relationships in Science and Technology, New Series II/11, edited by K.-H. Hellwege and A. Hellwege (Springer-Verlag, Berlin, 1981); C: -6 × 10⁻⁵; H: -2.93 × 10⁻⁵; O: -4.61 × 10⁻⁵; and the correction of the Ethel linkage: λ = -0.24 × 10⁻⁵ emu/mol. Empirically the calculated value would contain the error of ±5%-10%.

- [10] A.M. Clogston et al., Phys. Rev. Lett. 9, 262 (1962).
- [11] Normal Fermi Liquids, edited by D. Pines and P. Nozières, The Theory of Quantum Liquids Vol. I (W. A. Benjamin, New York, Amsterdam, 1966).
- [12] For the square lattice, we have $(1 + \lambda_{ep})N^*(E_F) \sim 0.31$ states/eV and $\lambda_{ep} \sim 0.19$ using $H_c = 995$ Oe (Ref. [7]). This is not meaningfully different from the case for the triangular lattice.
- [13] Various relations of the electron gas model with the dispersion relation, $E(k) = \hbar^2 k_r^2/(2m^*)$. For the 2D system $T_F^{2D} = \hbar^2 k_F^2/(2m^*k_B)$, $n_s^{2D} = k_F^2/(2\pi)$, $r_s^{2D} = 1/(\sqrt{2} a_B^*k_F)$, $k_{TF}^{2D} = 2/(a_B^*)$, and $\gamma^{2D} = \pi k_B^2 m^*/(3\hbar^2)$. For the 3D system, $T_F^{3D} = \hbar^2 k_F^2/(2m^*k_B)$, $n_s^{3D} = k_F^3/(3\pi^2)$, $r_s^{3D} = (9\pi/4)^{1/3}/(a_B^*k_F)$, $k_{TF}^{3D} = [4k_F/(\pi a_B^*)]^{1/2}$, and $\gamma^{3D} = k_B^2 m^* k_F/(3\hbar^2)$. Here, $a_B^* = \epsilon/(m^*e^2)$ is the effective Bohr radius and ϵ is the dielectric constant. For simplicity, we assumed $\epsilon = 1$. Especially for YBCO, we note that the present electron gas model may not be available because of the strong electronic correlation.
- [14] B. Batlogg *et al.*, Phys. Rev. Lett. **61**, 1670 (1988); M. Shirai, N. Suzuki, and K. Motizuki, J. Phys. Condens. Matter **2**, 3553 (1990); W. Jin *et al.*, Phys. Rev. B **45**, 5535 (1992); V. Meregalli and S. Savrasov, Phys. Rev. B **57**, 14453 (1998); H. J. Kaufmann *et al.*, Phys. Rev. B **58**, 9479 (1998); S. N. Barilo *et al.*, Phys. Rev. B **58**, 12355 (1998); P. Szabó *et al.*, Phys. Rev. B **62**, 3502 (2000).
- [15] J. W. Loram *et al.*, Phys. Rev. Lett. **71**, 1740 (1993); S. Shamoto *et al.*, J. Phys. Soc. Jpn. **63**, 2324 (1994); Y. Matsuda *et al.*, Phys. Rev. B **40**, 5176 (1989); D. N. Zheng *et al.*, Phys. Rev. B **49**, 1417 (1994).
- [16] L. P. Le et al., Phys. Rev. Lett. 68, 1923 (1992).
- [17] W. L. McMillan, Phys. Rev. 167, 331 (1968); P.B. Allen and R. C. Dynes, Phys. Rev. B 12, 905 (1975).
- [18] P. Morel and P. W. Anderson, Phys. Rev. 125, 1263 (1962).
- [19] If our assumption of the clean limit were not valid, then values in Table I would be modified as T_F = 18 800 K, k_F ~ 5.1 × 10⁷ cm⁻¹, k_{TF} ~ 11.1 × 10⁷ cm⁻¹, r_s ~ 7.1, μ* ~ 0.14, and λ_{ep} ~ 1.3 for the 3D model with carrier density fixed at n_s ~ 4.6 × 10²¹ cm⁻³ as calculated from the valency. Nevertheless both μ* > 0.14 and λ_{ep} > 1.3 are still too large and, in essence, do not differ from the clean limit case. This is because the localization effect may effectively enhance μ*, resulting in a large λ_{ep}. [H. Fukuyama, Physica (Amsterdam) 126B, 306 (1984)].
- [20] Y. Takada, J. Phys. Soc. Jpn. 45, 786 (1978); Phys. Rev. B 37, 155 (1988); 47, 5202 (1993); J. Phys. Soc. Jpn. 61, 238 (1992); H. Rietschel and L. J. Sham, Phys. Rev. B 28, 5100 (1983).