Arterial Mechanical Impedance is a Sensitive Stress Response Monitor During General Anesthesia

Ryuji NAKAMURA1), Noboru SAEKI1), Abdugheni KUTLUK2), Kenji SHIBA2), Toshio TSUJI2), Hiroshi HAMADA1) and Masashi KAWAMOTO1)
1) Department of Anesthesiology and Critical Care, Division of Clinical Medical Science, Graduate School of Biomedical Sciences, Hiroshima University, Kasumi 1-2-3 Minami-ku, Hiroshima 734-8551, Japan
2) Department of Artificial Complex Systems Engineering, Graduate School of Engineering, Hiroshima University, 1-4-1 Kagamiyama, Higashihiroshima 739-8527, Japan

ABSTRACT

Arterial mechanical impedance is a characteristic of arterial dynamics that is determined by photoplethysmographic amplitude and direct arterial pressure, while mechanical impedance is indicated by stiffness, viscosity, and inertia. We compared the parameters of mechanical impedance and photoplethysmographic amplitude to estimate the magnitude of stress response in patients undergoing general anesthesia by measuring direct arterial pressure. After sedating each patient with propofol, photoplethysmographic amplitude and mechanical impedance were measured as baseline control values, then 3 min after fentanyl administration (2 µg kg⁻¹), the parameters were measured again as post-fentanyl values. Thereafter, a direct laryngoscopy procedure was performed and post-laryngoscopy values for the parameters were determined. The magnitudes of response to each event were compared by using the ratio of the measurements from the preceding event. Then, comparisons of the magnitudes were performed after coordinating each response in the same direction. Our results showed that both stiffness and viscosity of mechanical impedance had greater variations than photoplethysmographic amplitude. In conclusion, we propose stiffness and viscosity derived from arterial mechanical impedance as sensitive parameters to monitor stress responses during general anesthesia.

Key words: Plethysmography, Autonomic response, Depth of anesthesia

General anesthetic agents and regional nerve blocks have been developed to suppress vital reactions against nociceptive stimuli during surgery. However, anesthesiologists must adjust the dosage of the anesthetics based mainly on clinical experience2,5,21). No established useful indicator has been presented that is effective for estimating stress response in order to determine the optimal dose of anesthetic agents, though some procedures to detect sympathetic nervous activity that are dependent on fingertip blood flow changes to titrate the dosage of anesthetic agents have been proposed7,12,18). We refer to the mechanical characteristics estimated by our methods as "mechanical impedance," which is shown by stiffness (K), viscosity (B), and inertia (M) (Fig. 1). Since this impedance is derived from a combination of PPG amplitude and DAP, we speculated that it may reflect stress response more accurately than PPG amplitude alone. There are no known reports that have compared mechanical impedance with PPG amplitude, thus we investigated the magnitude of mechanical impedance as an index of stress response and compared the results to PPG amplitude. In the present study, we administered fentanyl to reduce stress and performed a laryngoscopy to add stress, and then compared PPG amplitude response and mechanical impedance associated with each event.
The characteristics of the arterial wall were considered to be in an arbitrary radial direction. We assumed that arterial pressure was proportional to the force of blood flow and the photoplethysmogram result was proportional to the arterial radius. Components of mechanical impedance are shown as K, B, and M, which indicate stiffness, viscosity, and inertia, respectively.

**MATERIALS AND METHODS**

Consecutive patients who underwent elective surgery under general anesthesia with DAP measurements between May 1, 2006 and April 30, 2007 were enrolled in this study, after obtaining approval from our institutional Ethical Review Board and receiving written informed consent from each patient. Patients with the following conditions were excluded from enrollment: central nervous system disorder, sinus arrhythmia, moderate to severe aortic or tricuspid regurgitation, hemodialysis because of chronic renal insufficiency, autonomic disorder, or administration of psychotropic agents. We measured and recorded the parameters, as shown in Table 1.

Prior to inducing anesthesia, a bedside monitor (BSS-9800, NIHON KOHDEN, Tokyo, Japan) was used to acquire data. A photoplethysmogram probe (TL-271T, NIHON KOHDEN) was attached to the thumb of the measured upper limb and a catheter for measuring DAP was placed into the radial artery on the same side. A BIS monitoring system (A-2000™ BIS Monitoring System, Aspect Medical Systems, MA, USA) was also placed on the forehead. The environmental temperature was maintained at 24-27°C throughout the procedure. After completing the setting of these monitors, 1 mg of vecuronium or 5 mg of rocuronium was administered for precurarisation, and an intravenous infusion of 20-40 mg of lidocaine was given just before propofol administration to relieve injection pain. Propofol was administered using the TCI method with a syringe pump (TE-371, Terumo, Tokyo, Japan), which incorporated a Diprifusor (AstraZeneca Limited, London, UK). After confirming that the patient was asleep, the target concentration of the Diprifusor was regulated so that BIS was maintained within a range of 40-60, then 0.1 mg kg⁻¹ of vecuronium or 0.6 mg kg⁻¹ of rocuronium was administered, and artificial ventilation was maintained thereafter. The measurements were started when the difference between the estimated plasma concentration and estimated effect site concentration was less than 0.1, and at least 3 min after the DAP catheter was inserted to exclude a vasoconstrictor response against arterial puncture.

The outline of the study protocol is summarized in Fig. 2. After the baseline values were measured during propofol sedation (Control), Post-fentanyl values were obtained at 3 min after administration of 2 µg kg⁻¹ of fentanyl. The larynx was then examined by direct laryngoscopy to exclude patients with a difficult airway, assessed as Cormack grade III-IV. The values after the laryngoscopy (Post-LS) were determined for each parameter at the time of the lowest PPG amplitude for 1 min after the laryngoscopy procedure. The trachea was intubated after recording Post-LS values. When the entire anesthetic management was finished, any complications associated with the study procedures were recorded. PPG, DAP, and ECG waveforms were digitally recorded with a BSS-9800 at a sampling rate of 125 Hz using a personal computer, with BIS also digitally recorded by the computer every 5 sec. Hemoglobin concentration was measured once during the

**Table 1. Parameters measured in this study**

<table>
<thead>
<tr>
<th>Before anesthesia:</th>
<th>Age, gender, presence of hypertension, diabetes and hepatic cirrhosis, representative mean blood pressure, and pulse pressure for 3 preoperative days.</th>
</tr>
</thead>
<tbody>
<tr>
<td>PPG(Photoplethysmographic) waveform, DAP(direct arterial pressure) waveform, ECG(electrocardiographic) waveform, hemoglobin concentration, BIS value at time of control value acquisition, target concentration of Diprifusor at time of the control value acquisition.</td>
<td></td>
</tr>
<tr>
<td>At induction of anesthesia:</td>
<td>Presence of complication related to the study.</td>
</tr>
</tbody>
</table>

Fig. 1. Schema of arterial wall mechanical impedance model.
Arterial Impedance as a Stress Monitor

The estimated plasma concentration and effect site concentration of propofol, K (stiffness of arterial wall), and PPG (photoplethysmogram) amplitude were displayed in a three-part ordinate. The abscissa represents the time course, while 3 measurement points (Control, Post-fentanyl, and Post-LS) are displayed by alternating long and short dashed vertical lines. K and PPG amplitude represent values before normalization, thus the units of the ordinate are arbitrary.

Post-fentanyl: after fentanyl administration, Post-LS: after laryngoscopy induction of anesthesia.

Enrolled patients with difficult mask ventilation or arrhythmia, and those that required vasopressors for a mean blood pressure below 60 mmHg over 5 min were excluded from the present analysis. Recorded data were analyzed offline using LabVIEW 7.0 (National Instruments, Austin, Texas, United States). Data with mixed noise at the 3 measurement points (Control, Post-fentanyl, and Post-LS) were excluded from analysis. For analysis of the data, the peak of the R wave detected from the ECG waveform was assumed to be the initiation moment of each heartbeat. Both PPG and DAP waveforms were analyzed beat-by-beat, and PPG amplitude and each parameter of mechanical impedance (K, B and M) were computed (Appendix).

The measured mechanical impedance parameters K, B, and M were 'normalized' by dividing the Post-fentanyl and Post-LS values by each Control value, which yielded normalized K (nK), normalized B (nB), and normalized M (nM), respectively. Based on the formula presented in the Appendix, mechanical impedance and PPG amplitude were assumed to change in an inverse manner. Namely, arterial resistance, which was expressed as mechanical impedance, and blood flow, which was proportional to PPG amplitude, were considered to be inversely altered. Normalized PPG amplitude (nPPG) was also obtained by dividing the Control value by the Post-fentanyl and Post-LS values.

To compare the magnitude of response to each event among the parameters, we used the ratio between the pre- and post-values for each parameter. The response of fentanyl administration was determined using normalized values at Post-fentanyl, which were divided by the normalized values at Post-LS to determine 'laryngoscopy response' (Post-/Pre-LS).

Based on a preliminary study of 10 patients, we calculated that a sample size of 96 and 78 patients for Post-fentanyl and Pre/Post-LS, respectively, would give a 5% difference between nPPG and nK, with a power of 80%. Since cases that could not be analyzed because of noise were estimated to be approximately 5%, we planned to collect data from 100 patients. Statistical analysis was performed using SPSS (SPSS Japan Inc., Tokyo, Japan). Multiple regression analysis was done to evaluate the factors that influenced measured and normalized value of PPG amplitude, K, B, and M. The objective variables were measured values (PPG amplitude, K, B, and M at Control, Post-Fentanyl and Post-LS) and normalized values (nPPG, nK, nB, and nM at Post-fentanyl and Post-LS). Dependent variables included age, gender, presence of hypertension, diabetes and cirrhosis, hemoglobin concentration, BIS, and targeted propofol concentration, which were selected by the Stepwise method. When the F probability of the dependent variable was 0.05 or less, the
dependent variable was adopted, while the dependent variable was removed when the F probability of the dependent variable was 0.10 or greater. Standardized partial regression coefficients of the adopted dependent variables and determination coefficients were obtained. When performing comparisons of measurements between events, PPG amplitude, K, B, and M at Control, Post-fentanyl and Post-LS were compared within each parameter. When comparisons were conducted between parameters, the response of PPG amplitude, K, B, and M at fentanyl administration and laryngoscopy were compared within each event. Comparisons were performed using a Wilcoxon signed-rank test with Bonferroni's correction and the level of significance was set at p<0.05.

RESULTS

A total of 111 patients were enrolled in this study, with 11 excluded from registration for receiving vasopressors (n=5), difficult mask ventilation (n=4), and arrhythmia (n=2). Of the 100 registered patients, 6 were excluded from analysis because of contaminating noise. Thus, demographic data from the remaining 94 patients (Table 2), and the determination coefficients for each measurement and standard regression coefficients of the dependent variables (Table 3) are presented. Though all parameters of Control and Post-fentanyl and PPG amplitude and B of Post-LS had a significant regression model, nK and nB did not have a significant regression model. Gender, presence of hypertension, and presence of liver cirrhosis were significantly related

Table 2. Preoperative characteristics and perioperative measurements

<table>
<thead>
<tr>
<th>Age (years)</th>
<th>Gender (Male/Female)</th>
<th>Hypertension (Yes/No)</th>
<th>Diabetic mellitus (Yes/No)</th>
<th>Liver cirrhosis (Yes/No)</th>
<th>MBP (mmHg)</th>
<th>PP (mmHg)</th>
<th>Hb (g dl⁻¹)</th>
<th>BIS</th>
<th>Propofol target concentration (ng ml⁻¹)</th>
</tr>
</thead>
<tbody>
<tr>
<td>63.2±13.2</td>
<td>72/22</td>
<td>25/69</td>
<td>20/74</td>
<td>22/72</td>
<td>85.1±11.0</td>
<td>52.0±14.0</td>
<td>11.5±1.8</td>
<td>47.7±10.9</td>
<td>2.5±0.5</td>
</tr>
</tbody>
</table>

Values shown represent the mean (SD) or a number (n). MBP, mean blood pressure for 3 preoperative days; PP, pulse pressure for 3 preoperative days; Hb, hemoglobin measured at the induction of anesthesia; BIS and targeted propofol concentration were obtained at the time of Control value acquisition for each subject.

Table 3. Multiple regression analysis results

<table>
<thead>
<tr>
<th>Objective</th>
<th>Coefficient of</th>
<th>Standard partial regression coefficient of each dependent variable</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>determination</td>
<td>Age</td>
</tr>
<tr>
<td>Measured</td>
<td></td>
<td></td>
</tr>
<tr>
<td>values</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Control</td>
<td>PPG</td>
<td>0.05</td>
</tr>
<tr>
<td>K</td>
<td>0.1</td>
<td>-</td>
</tr>
<tr>
<td>B</td>
<td>0.18</td>
<td>0.07</td>
</tr>
<tr>
<td>M</td>
<td>0.18</td>
<td>0.22</td>
</tr>
<tr>
<td>Post-fentanyl</td>
<td>PPG</td>
<td>0.11</td>
</tr>
<tr>
<td>K</td>
<td>0.15</td>
<td>0.24</td>
</tr>
<tr>
<td>B</td>
<td>0.18</td>
<td>0.28</td>
</tr>
<tr>
<td>M</td>
<td>0.08</td>
<td>0.28</td>
</tr>
<tr>
<td>Post-LS</td>
<td>PPG</td>
<td>0.09</td>
</tr>
<tr>
<td>K</td>
<td>-</td>
<td>-</td>
</tr>
<tr>
<td>B</td>
<td>-</td>
<td>-</td>
</tr>
<tr>
<td>M</td>
<td>-</td>
<td>-</td>
</tr>
<tr>
<td>Normalized</td>
<td>nPPG</td>
<td>0.05</td>
</tr>
<tr>
<td>K</td>
<td>-</td>
<td>-</td>
</tr>
<tr>
<td>B</td>
<td>-</td>
<td>-</td>
</tr>
<tr>
<td>M</td>
<td>-</td>
<td>-</td>
</tr>
<tr>
<td>Post-Fentanyl</td>
<td>nPPG</td>
<td>0.04</td>
</tr>
<tr>
<td>K</td>
<td>-</td>
<td>-</td>
</tr>
<tr>
<td>B</td>
<td>-</td>
<td>-</td>
</tr>
<tr>
<td>M</td>
<td>-</td>
<td>-</td>
</tr>
</tbody>
</table>

The coefficients of determination for measured values and normalized values of PPG amplitude, K, B, and M for the Control, Post-fentanyl and Post-LS measurements are shown. Each row shows each regression model. The dependent variables removed from regression had no standard partial regression coefficient. The regression without the coefficient of determination had no significant regression model. PPG, amplitude of photoplethysmogram; K, stiffness of arterial wall; B, viscosity of arterial wall; M, inertia of arterial wall; nPPG, normalized PPG amplitude; nK, normalized K; nB, normalized B; nM, normalized M; HT, presence of hypertension; DM, presence of diabetes mellitus; LC, presence of liver cirrhosis; Hb, hemoglobin measured at the induction of anesthesia; BIS, BIS obtained at the time of Control value acquisition for each subject; Propofol, targeted propofol concentration obtained at the time of Control value acquisition for each subject.
to nPPG and nM, with the determination coefficients of these parameters found to be 0.04 and 0.05, respectively. As shown in Fig. 3, all of the parameters decreased significantly to lower than the Control values at Post-fentanyl, whereas PPG amplitude, K and B, but not M, at Post-LS were increased significantly to values higher than the Control and Post-fentanyl values. Figure 4 shows the magnitudes of responses at each event for the parameters. Administration of fentanyl caused significantly smaller responses for nK, nB, and nM, as compared to nPPG, while there were no significant differences among nK, nB, and nM. Responses at laryngoscopy showed that the responses of nK and nB were larger than that of nPPG. In addition, the response of nM was smaller than all of the other parameters. There was no significant difference between nK and nB.

**DISCUSSION**

In the present study, nPPG, nK, and nB were decreased after fentanyl administration and increased by performance of a laryngoscopy. In addition, the responses of nK and nB to the administration of fentanyl and laryngoscopy were significantly greater than that of nPPG, which suggests that nK and nB have a greater response to stress than nPPG.

Differences in absorptive biological tissues, such as skin pigmentation, fibrous protein, collagen and fat, the contacting force between finger and probe, and blood hemoglobin concentrations, are factors known to affect photoplethysmogram results. In addition, it is considered that the bloodstream is affected by vascular endothelial function or autonomic nervous system function. However, except for autonomic nervous system function, none of elements thought to have effects on photoplethysmogram and bloodstream in the finger were altered during the present study period. Therefore we normalized all measurements for each patient to eliminate the effects of those elements, except for that of the autonomic nervous system, on bloodstream changes. Our results showed that all of the dependent variables were unrelated to nK and nB. Furthermore, the coefficients obtained by multiple regression analyses of nPPG and nM were negligible. These results suggest that normalized values for PPG amplitude and mechanical impedance, especially nK and nB, are robust against the differences of age, gender, or presence of complications adopted in this study.

Fig. 3. Changes in measured values including PPG amplitude, K, B, and M, at Control and after fentanyl administration and laryngoscopy. Each line connects the measured values of each patient. Though Control values of all parameters have wide dispersion, most patients changed in same direction between events in PPG amplitude, K, and B. K, stiffness of arterial wall; B, viscosity of arterial wall; M, inertia of arterial wall. *p<0.05
We found that nK and nB were decreased by a greater degree than nPPG upon fentanyl administration. Administration of fentanyl under propofol anesthesia causes a reduction in blood pressure, systemic vascular resistance, and cardiac output\(^2,25,26\). When blood flow is considered as a slow viscous constant flow through a tube, it is proportional to blood pressure and inversely proportional to the fourth power of the radius according to Hagen-Poiseuille’s law. In other words, a decrease in blood pressure reduces blood flow, while reduction of vascular resistance induced by vasodilation increases blood flow. A photoplethysmogram reflects blood flow in the systemic vascular resistance, and cardiac output together with it. Based on our results, we propose that both nK and nB be considered as new stress response monitors that are more sensitive than nPPG.

Unlike K and B, M did not change with laryngoscopy stimulation. M is a parameter that indicates inertia in mechanical impedance, while inertia in a vascular mechanical impedance model represents the change in density per unit of area in the radial direction of the vessel walls. Vasoconstriction increases vascular wall density per area unit by smooth muscle contraction. However, this change is considered to be extremely small, thus it is not clear whether a change in inertia by dilation or contraction is actually detectable. In our study, M was decreased upon fentanyl administration, whereas no significant change was observed with the laryngoscopy, suggesting that this parameter is not useful for monitoring stress response.

In the present study, sampled values were normalized by calculating the ratio of each measurement relative to the Control value. However, since Control values were determined for each subject and differed among them, we could not compare the magnitude of stress response among the subjects. In previous evaluations of stress response, a surgical stress index was proposed\(^6,22\) in which PPG amplitude was the main element, as in the present study. The surgical stress index normalizes each value with a reference value\(^6\), a part of which is determined by the measured value of each patient, while the remaining values are determined based on a data pool collected from other patients. In contrast, we did not use a data pool of measurements obtained from other patients to determine the individual Control values for patients, because the individual differences in PPG amplitude and mechanical impedance were large and irregular. In order to develop a monitoring method that can compare stress responses among patients, it is important to develop a normalization method that is much less dependent on individual patients.

When a blood vessel shrinks blood pressure increases, thereby increasing the tension of the vessel walls. If a blood vessel is considered to be structured like an elastic pipe, it is expected that both stiffness and viscosity will increase when the vessel shrinks. In the present study, nK and nB

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**Fig. 4.** Comparison of magnitudes of responses between parameters.

The magnitudes of responses to each event were compared by determining the ratio of normalized values from preceding event values. The ordinate was expressed as a log scale. Boxes and center lines indicate interquartile range and median value, respectively. Whiskers show minimum and maximum ranges.

- nPPG, normalized photoplethysmogram amplitude;
- nK, normalized stiffness of arterial wall;
- nB, normalized viscosity of arterial wall;
- nM, normalized inertia of arterial wall.

*p<0.05 in comparison with the other parameters. **p<0.05 in comparison with nK and nB.
showed similar changes, and their clinical meaning could not be distinguished, thus further studies are needed.

In the present study, correlations between all parameters and dependent variables were low. Since the variability of \( nK \) and \( nB \) after performance of fentanyl administration and a laryngoscopy were much greater than that of nPPG, we propose that both \( nK \) and \( nB \) are sensitive stress response indicators.

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APPENDIX

1. Modeling arterial dynamic characteristics.

We propose a procedure to estimate the characteristics of arterial dynamics using a mechanical impedance model. In this method, which considers only the characteristics of the arterial wall in an arbitrary radial direction, the impedance characteristics can be expressed based on radial force and wall displacement, as follows:

\[
F(t) = Md\ddot{r}(t) + B\dot{r}(t) + K(r(t) - r_0) \tag{1}
\]

where \( F(t) \) is the force of the blood flow on the arterial wall, and \( M, B, \) and \( K \) represent inertia, viscosity, and stiffness, respectively; \( r(t), \dot{r}(t), \ddot{r}(t) \) are the position, velocity, and acceleration of the arterial wall, respectively, and \( r_0 \) is the arterial radius with zero pressure. When using \( t_0 \) to denote the start time of displacement, the dynamic characteristics of the blood vessel at time \( t \) are expressed as follows:

\[
dF(t) = Md\ddot{r}(t_0) + B\dot{r}(t_0) + K\dot{r}(t_0) \tag{2}
\]

where \( dF(t) \) is the sum of all arterial radii at the measurement location.

The electrocardiogram, invasive arterial pressure \( P(t) \), and photoplethysmogram \( P(t) \) were simultaneously measured. All \( P(t) \) were interpreted as noise contaminated data and excluded. In this study, we describe \( K, B, M \) as \( K, B, M \) and \( r(t) \) is the arterial radius proportional constant and \( r(t) \) is the sum of all arterial radii at the measurement location.

2. Photoplethysmogram.

Directly measuring \( r(t) \) is difficult in a clinical setting. Therefore, the arterial radius is estimated from a photoplethysmogram with this protocol. Using Lambert-Beer's law, the change in absorbance \( \Delta A(t) \) can be expressed as follows:

\[
\Delta A(t) = A(t) - A_0 = \log \left( I_o / (I_o - \Delta I(t)) \right) = ECD(t) \cdot \Delta D(t) \tag{4}
\]

where \( A(t) \) is absorbance, \( A_0 \) is absorbance due to the arterial diameter of \( D \), \( C \) is the density of light absorbing material, \( D \) is the arterial diameter, \( E \) is an absorbance constant unique to the material, \( I_o \) is the intensity of transmitted light on a blood vessel with diameter \( D \), and \( \Delta D(t) \) is the change in arterial diameter. A photoplethysmogram measures \( \Delta A(t) \). When simply assuming that the arterial radius is proportional to the photoplethysmogram, then the photoplethysmogram \( P(t) \) can be expressed as follows:

\[
P(t) = k_p r(t) \tag{5}
\]

where \( k_p \) is a proportionality constant and \( r(t) \) is the arterial radius.

3. Impedance model.

Using arterial pressure \( P(t) \) (of (3)) as the force acting on the arterial wall and photoplethysmogram \( P(t) \) (of (5)) for the arterial radius, arterial wall impedance is estimated from the following equation:

\[
dP(t) = \tilde{K} \dot{P}(t) + \tilde{B} \dot{P}(t) + \tilde{M} \ddot{P}(t) \tag{6}
\]

where

\[
\tilde{K} = K/k_p, \tilde{B} = B/k_p, \tilde{M} = M/k_p
\]

and

\[
dP_0(t) = P_0(t) - P_0(t_0), \quad dP(t) = P(t) - P(t_0), \quad d\dot{P}(t) = \dot{P}(t_0) - \dot{P}(t)
\]

4. Fitting

In this method, the impedance parameters \( K, B, M \) are estimated using \( P_0(t) \) and \( P(t) \). The electrocardiogram, invasive arterial pressure \( P_0(t) \), and photoplethysmogram \( P(t) \) were simultaneously measured. All \( P_0(t) \) and \( P(t) \) values obtained in the interval between the R wave and subsequent R wave were used as a dataset. Impedance parameters were estimated by least square fitting using a dataset and (6). Without noisy waveform data, almost all of the correlation coefficient of real \( P(t) \) and estimated \( P(t) \) was greater than 0.95. Therefore, if the correlation coefficient of a dataset was under 0.95, the dataset was interpreted as noise contaminated data and excluded. In this study, we describe \( K, B, M \) as \( K, B, M \) and \( \) respectively.
REFERENCES


